# Can we improve descriptions of nuclear effects in neutrino interactions using electron-scattering data?

Artur M. Ankowski Center for Neutrino Physics, Virginia Tech

> Fermilab Neutrino Seminar May 11, 2017

#### **Outline**

#### 1) Introduction

- Why do we need to model nuclear effects accurately?
- What can we learn from electron scattering?

#### 2) Spectral function approach

- Short-range correlations
- Are final-state interactions relevant?

#### 3) Measurement of the spectral function of 40Ar

- Physics motivation
- Coincidence electron scattering and the spectral function

#### 4) Summary

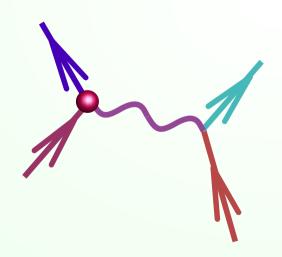


**Energy reconstruction** 

#### Kinematic reconstruction

In quasielastic scattering off **free nucleons**,  $v + p \rightarrow l + n$  and  $v + n \rightarrow l + p$ , we can deduce the neutrino energy from the charged lepton's kinematics.

No need to reconstruct the nucleon kinematics.

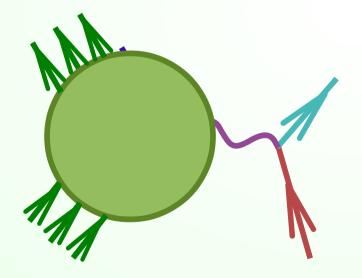


E' and  $\theta$  known

$$E = \frac{ME' + \text{const}}{M - E' + |\mathbf{k}'| \cos \theta}$$

#### **Kinematic reconstruction**

In nuclei the reconstruction becomes an approximation due to the binding energy, Fermi motion, final-state interactions, two-body interactions etc.

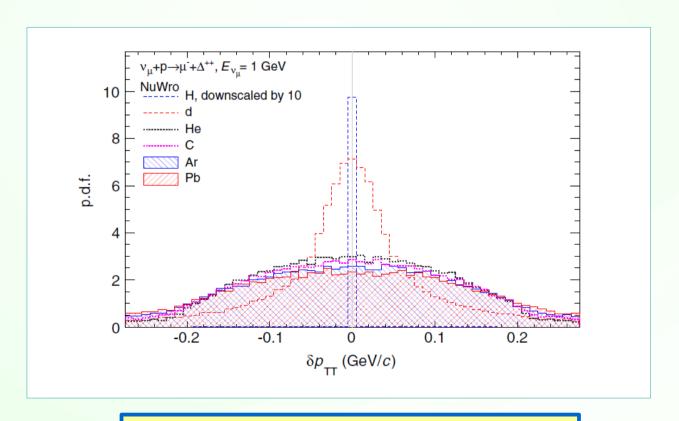


E' and  $\theta$  known

$$E \simeq \frac{(M - \epsilon)E' + \text{const}}{M - \epsilon - E' + |\mathbf{k}'| \cos \theta}$$

# **Free-proton events**

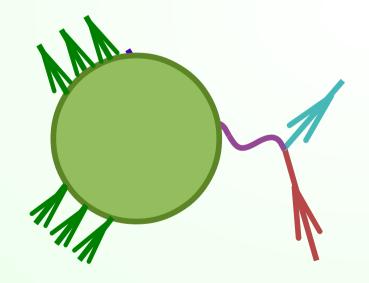
For targets containing H, the ( $\nu$  and  $\nu$ ) pion-production events on free protons could be separated out, based on the balance of the transverse momentum.



Lu et al., PRD 92, 051302 (2015)

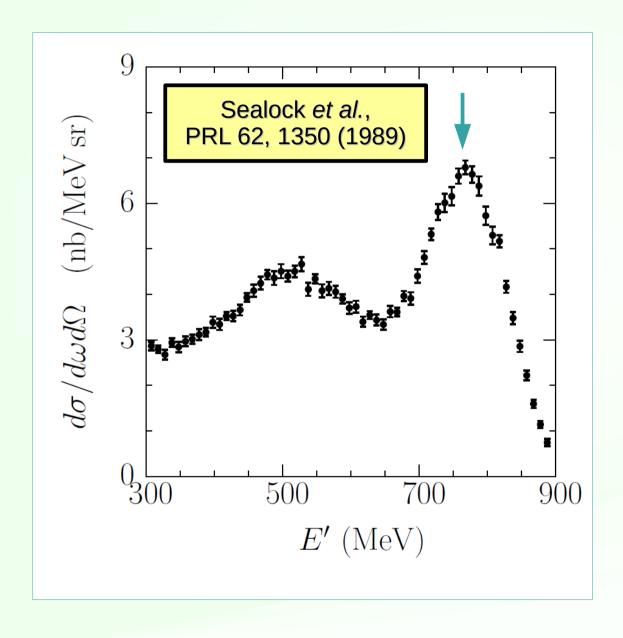
Consider the simplest (unrealistic) case:

the beam is monochromatic but its energy is unknown and has to be reconstructed

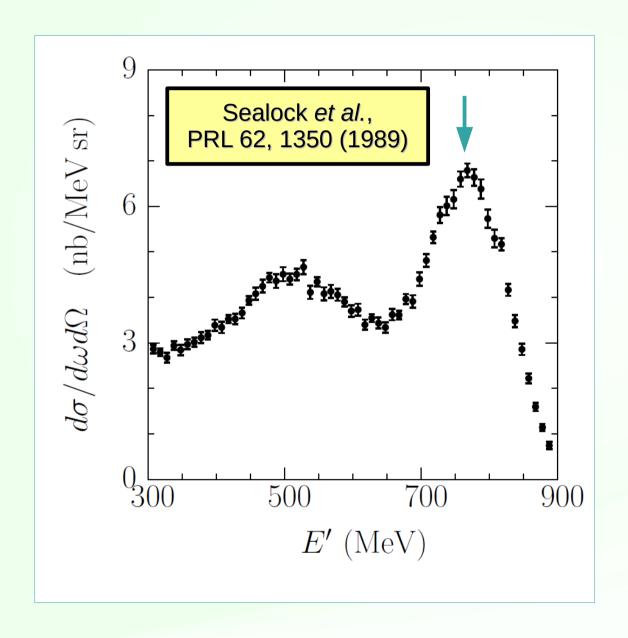


E' and  $\theta$  known

$$E=?$$

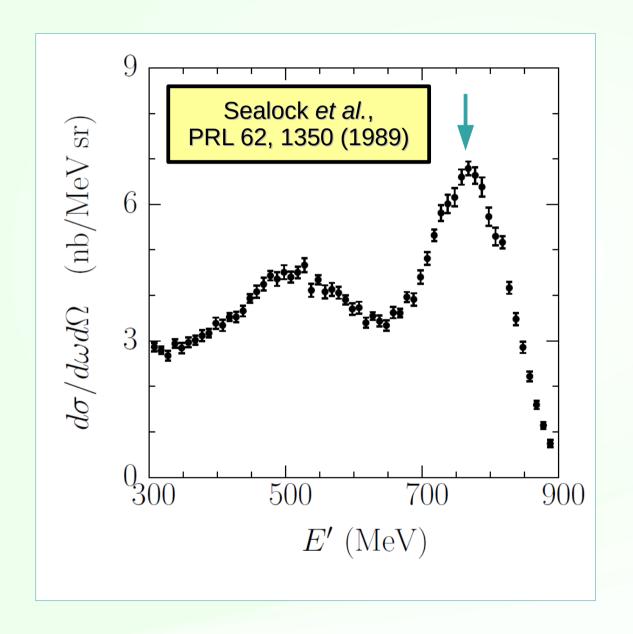


$$E' = 768 \text{ MeV}$$
  
 $\theta = 37.5 \text{ deg}$   
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for 
$$\epsilon = 25$$
 MeV  
 $E = 960$  MeV  
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 $true\ value$   $E = 961\ MeV$ 

$\theta$ (deg)	37.5	37.5	37.1	36.0	36.0
E' (MeV)	976	768	615	487.5	287.5
$\Delta E'$ (MeV)	5	5	5	5	2.5

Assuming  $\epsilon = 25 \text{ MeV}$ 

rec. E	$1285 \pm 8$	$960 \pm 7$	741 ± 7	$571 \pm 6$	$333 \pm 3$
true E	1299	961	730	560	320

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#### Appropriate $\epsilon$ value?

true E	1299	961	730	560	320
$\epsilon$	$33 \pm 5$	$26 \pm 5$	$16 \pm 5$	$16 \pm 3$	$13 \pm 3$

Sealock et al., PRL 62, 1350 (1989) O'Connell *et al.*, PRC 35, 1063 (1987) Barreau *et al.*, NPA 402, 515 (1983)

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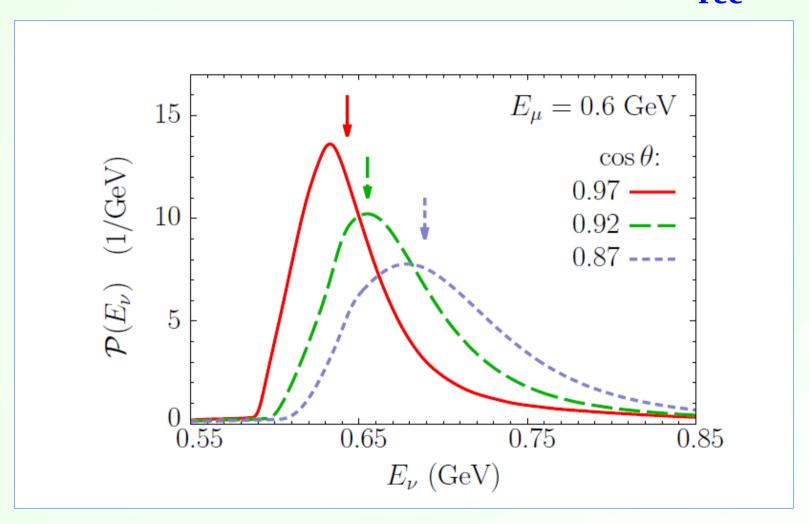
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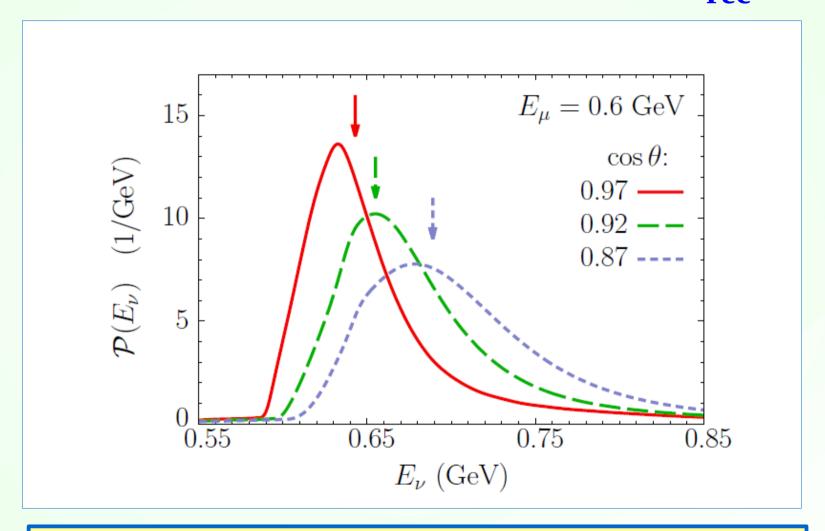
different 
$$E \equiv \text{different } Q^2 \equiv \text{different } \theta$$

$$\rightarrow \text{different } \epsilon$$

# Realistic calculations vs $\boldsymbol{E}_{\mathrm{rec}}$



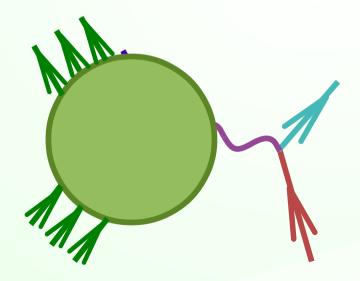
# Realistic calculations vs $E_{rec}$



Same physics drives the QE peak position and relates the kinematics to neutrino energy

# Polychromatic beam

In modern experiments, the neutrino beams are not monochromatic, and the **energy must be reconstructed** from the observables, typically E' and  $\cos \theta$  under the CCQE event hypothesis.



E' and  $\theta$  known

$$E = ?$$

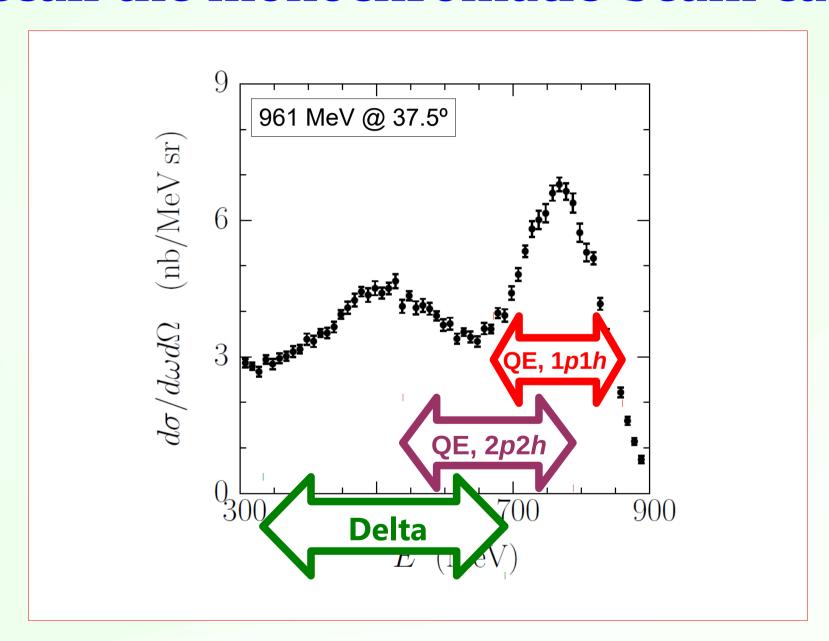
### **CCQE** events

In practice, CCQE event candidates are defined as containing no pions observed.

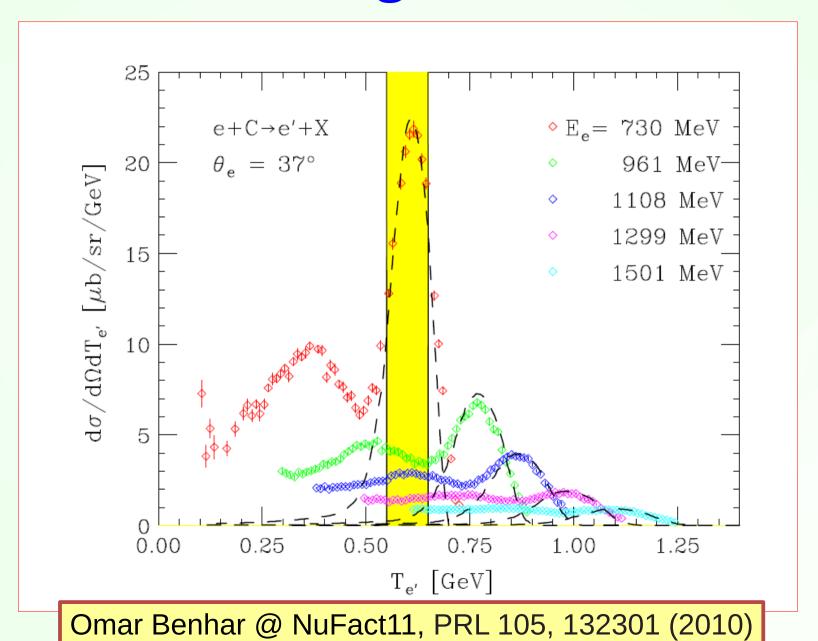
- CCQE (any number of nucleons)
- + pion production and followed by absorption undetected pions
- CCQE with pions from FSI

 $0\pi$  events

## Recall the monochromatic-beam case



# CCQE events of given *l*<sup>±</sup> kinematics



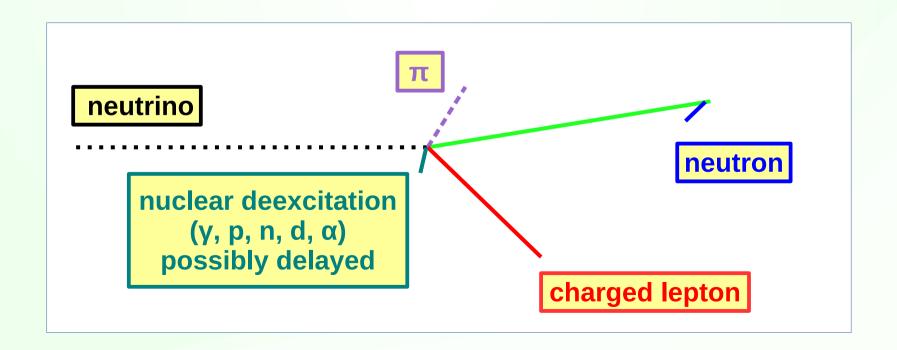
# Calorimetric energy reconstruction

- Advantage: applicable to any final states
- Insensitive to nuclear effects when

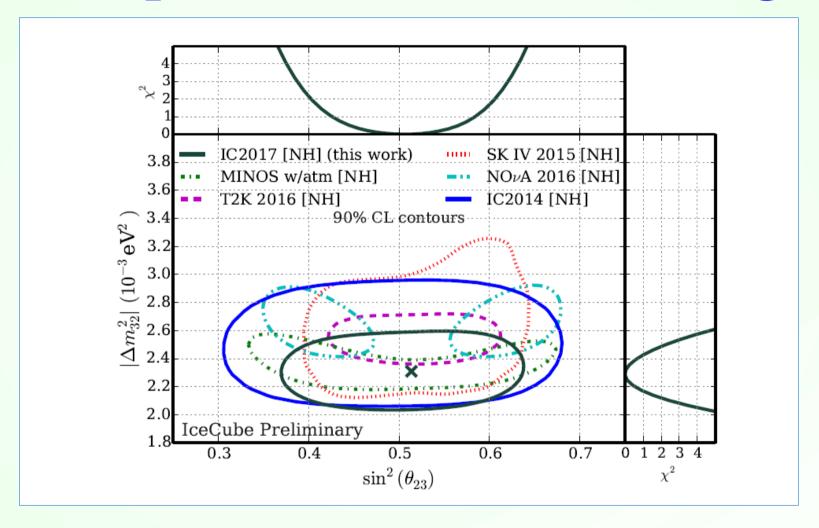
missing energy « neutrino energy

A.M.A., arXiv: 1704.07835

Otherwise, requires input from nuclear models



# What precision are we reaching?



J. Hignight (IceCube), APS April Meeting, 2017

# What precision are we reaching?

At the T2K kinematics (~600 MeV),

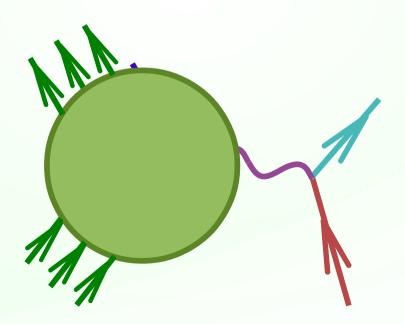
- 10% uncertainty (current T2K), ~60 MeV
- 2% uncertainty (current global fits), ~10 MeV

At the NOvA and DUNE kinematics, values x4-5.

Effects considered to be "small" need to be accounted for accurately to avoid biases.

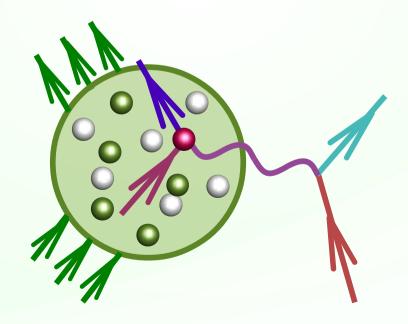


Assumption: the dominant process of lepton-nucleus interaction is scattering off a single nucleon, with the remaining nucleons acting as a spectator system.



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It is valid when the momentum transfer  $|\mathbf{q}|$  is high enough, as the probe's spatial resolution is  $\sim 1/|\mathbf{q}|$ .

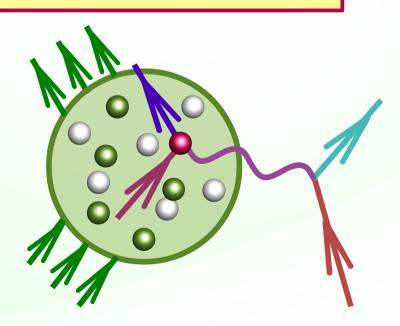


$$\frac{d\sigma_{\ell A}^{\text{IA}}}{d\omega d\Omega} = \sum_{N} \int d^{3}p \, dE \, P_{\text{hole}}^{N}(\mathbf{p}, E) \, \frac{M}{E_{\mathbf{p}}} \frac{d\sigma_{\ell N}^{\text{elem}}}{d\omega d\Omega} \, \underline{P_{\text{part}}^{N}(\mathbf{p}', \mathcal{T}')}$$

Spectral function

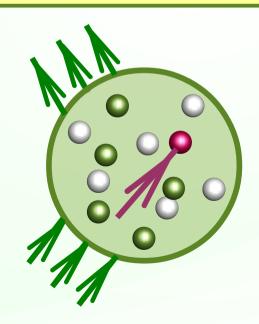
 $\sim \delta(...)$  x Pauli blocking

Elementary cross section



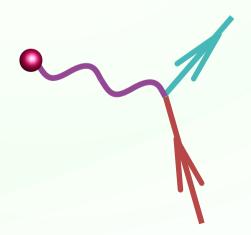
$$\frac{d\sigma_{\ell A}^{\text{IA}}}{d\omega d\Omega} = \sum_{N} \int d^{3}p \, dE \, P_{\text{hole}}^{N}(\mathbf{p}, E) \, \frac{M}{E_{\mathbf{p}}} \frac{d\sigma_{\ell N}^{\text{elem}}}{d\omega d\Omega} \, P_{\text{part}}^{N}(\mathbf{p}', \mathcal{T}')$$

The (hole) spectral function describes the ground-state properties of the target nucleus.



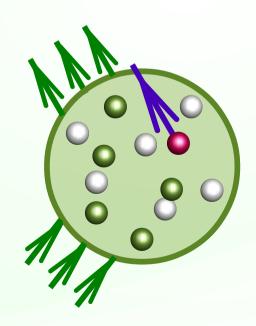
$$\frac{d\sigma_{\ell A}^{\text{IA}}}{d\omega d\Omega} = \sum_{N} \int d^{3}p \, dE \, P_{\text{hole}}^{N}(\mathbf{p}, E) \, \frac{M}{E_{\mathbf{p}}} \frac{d\sigma_{\ell N}^{\text{elem}}}{d\omega d\Omega} \, P_{\text{part}}^{N}(\mathbf{p}', \mathcal{T}')$$

The elementary cross section characterizes the vertex



$$\frac{d\sigma_{\ell A}^{\text{IA}}}{d\omega d\Omega} = \sum_{N} \int d^{3}p \, dE \, P_{\text{hole}}^{N}(\mathbf{p}, E) \, \frac{M}{E_{\mathbf{p}}} \frac{d\sigma_{\ell N}^{\text{elem}}}{d\omega d\Omega} \, \underline{P_{\text{part}}^{N}(\mathbf{p}', \mathcal{T}')}$$

Ensures the energy conservation and Pauli blocking

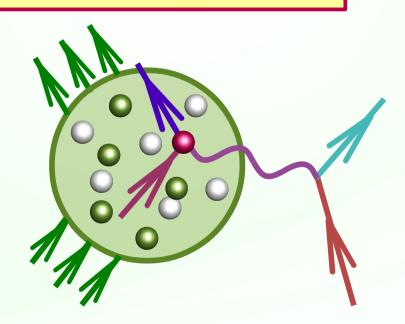


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Spectral function

 $\sim \delta(...)$  x Pauli blocking

Elementary cross section

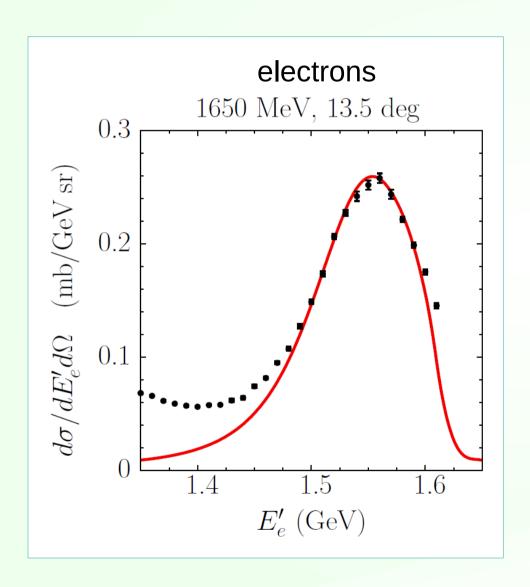


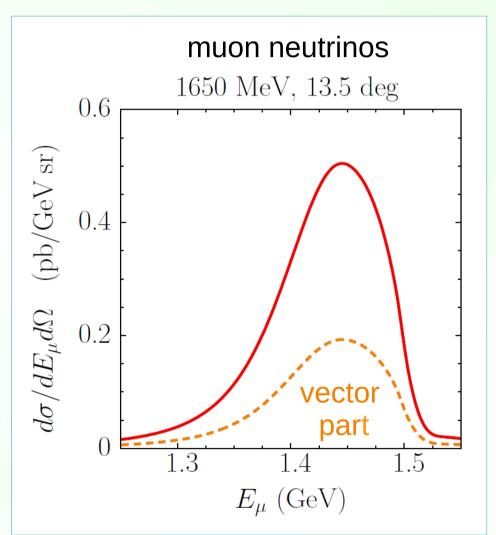
For scattering in a given angle, neutrinos and electrons differ only due to the elementary cross section.

In neutrino scattering, uncertainties come from (i) interaction dynamics and (ii) nuclear effects.

It is **highly improbable** that theoretical approaches unable to reproduce (e,e') data would describe nuclear effects in neutrino interactions at similar kinematics.

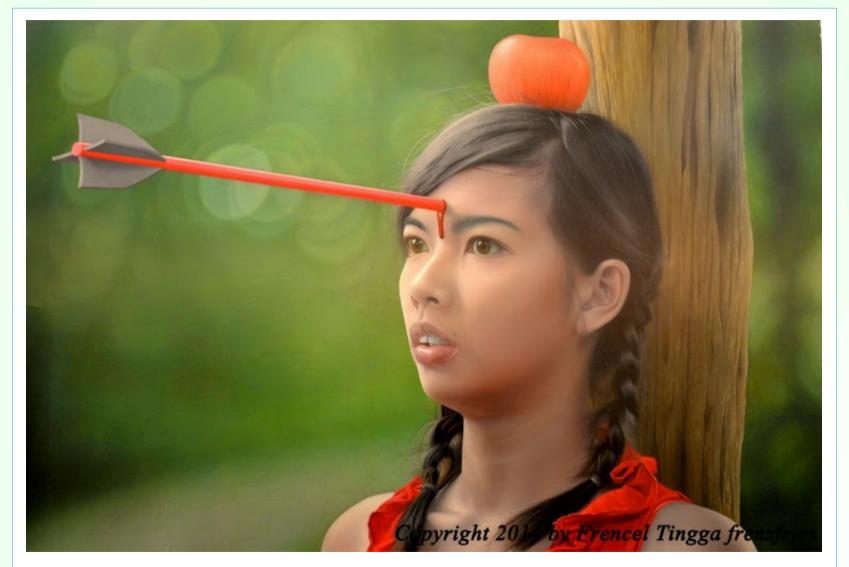
# Much more than the vector part...





# Can we trust our models and MCs?

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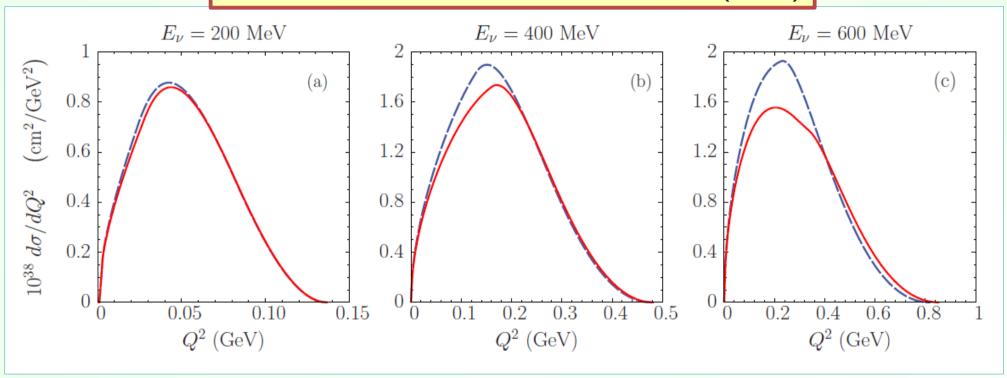


"Trusting Too Much Kills You" by Bryan Teves

and lacking precision

#### Side remark: relativistic kinematics

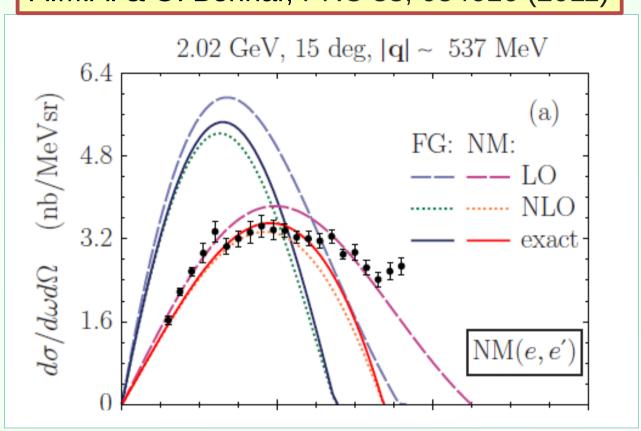
A.M.A. & O. Benhar, PRC 83, 054616 (2011)



Sizable differences between the **relativistic** and **nonrelativistic** results at neutrino energies ~500 MeV.

#### Side remark: relativistic kinematics

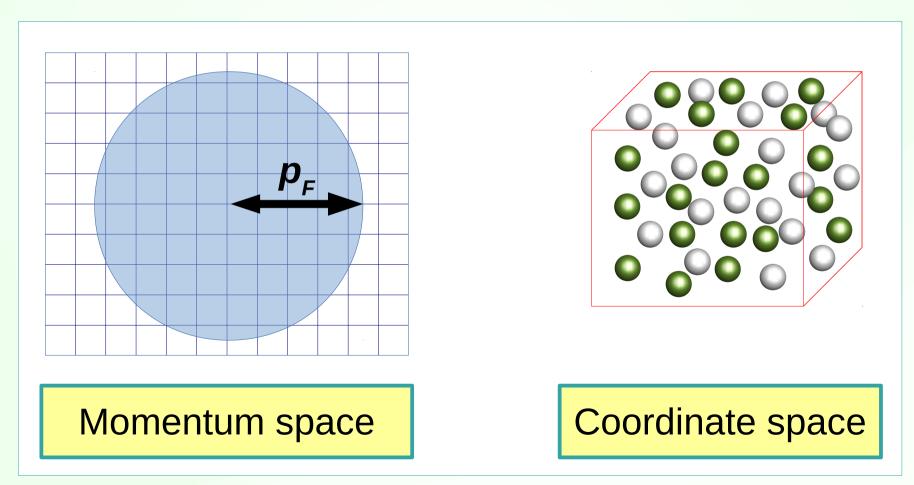
A.M.A. & O. Benhar, PRC 83, 054616 (2011)



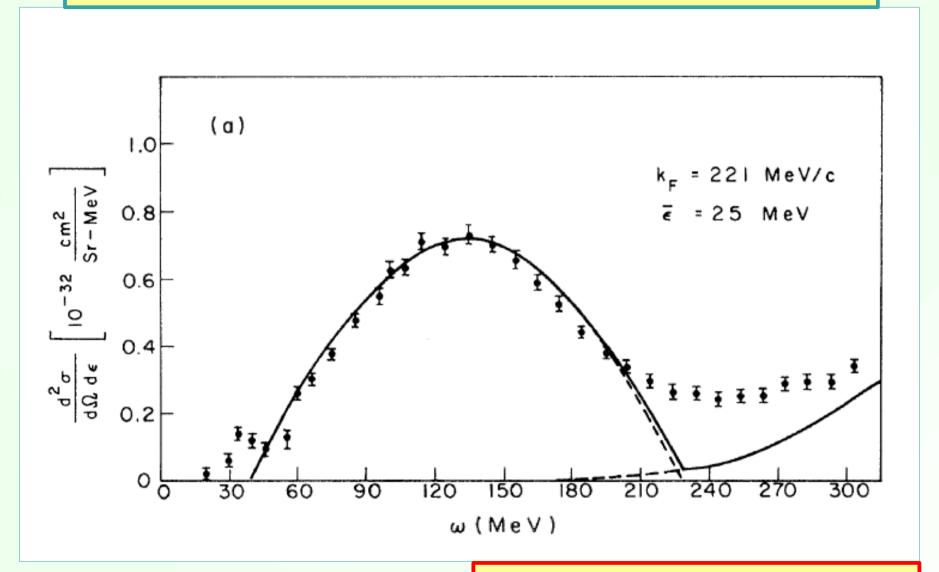
At |q|~540 MeV, semi-relativistic result is 5% lower than the exact cross section.

#### Fermi gas model

In an infinite infinite space filled uniformly with nucleons, the eigenstates can be labeled using the momentum.

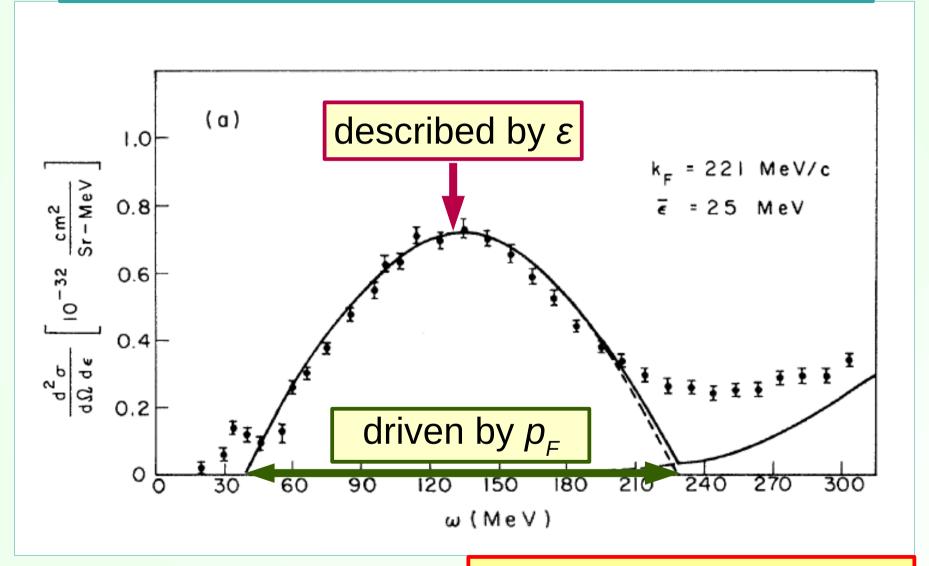


#### Electron scattering off carbon, 500 MeV, 60 deg



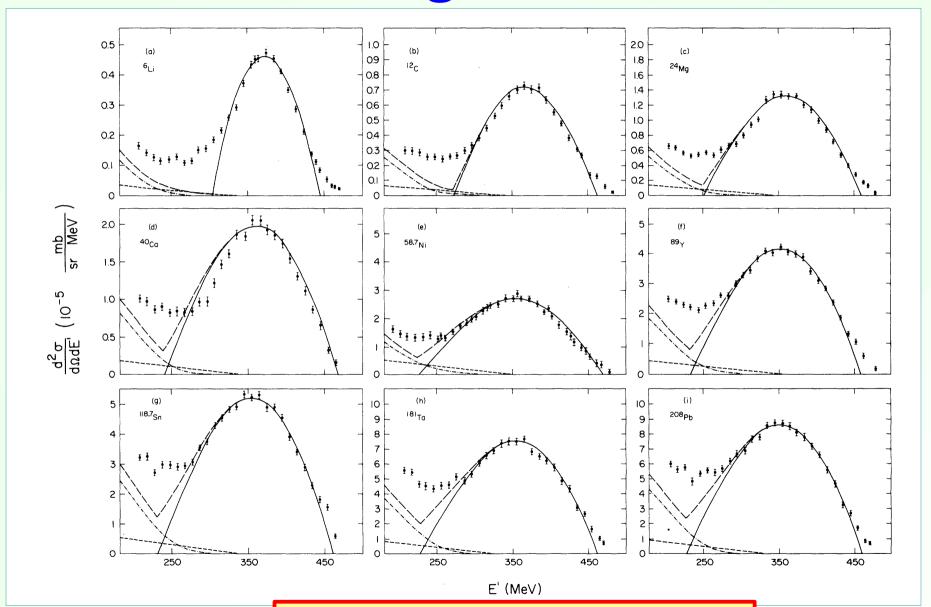
Moniz et al., PRL 26, 445 (1971)

#### Electron scattering off carbon, 500 MeV, 60 deg



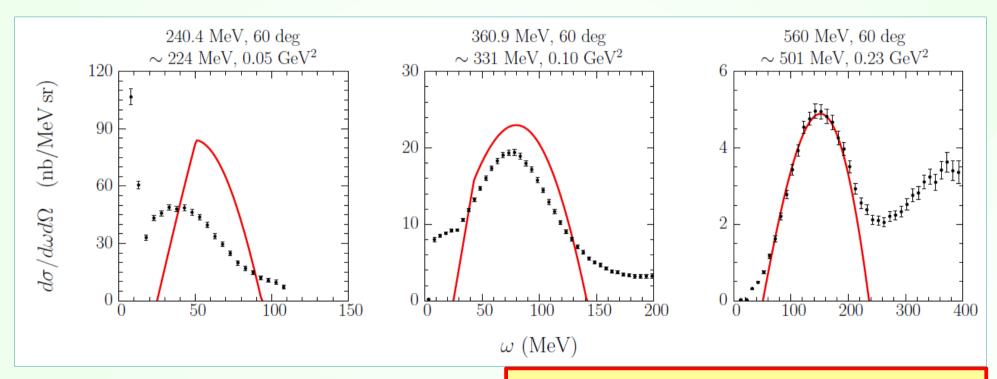
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# Fermi gas model



# Fermi gas model

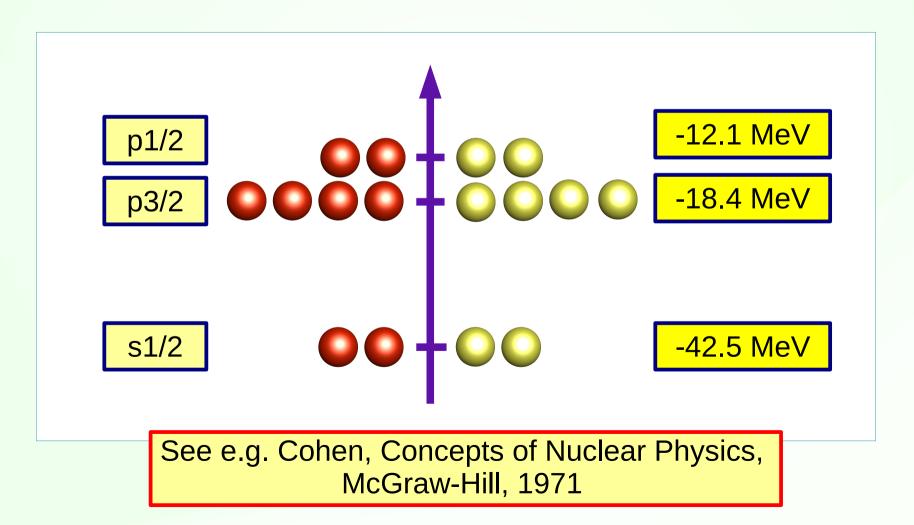
What happens at kinematics other than 500 MeV, 60 deg?



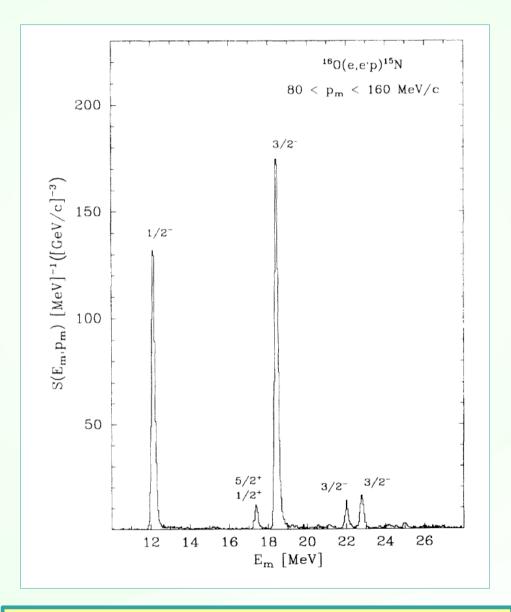
Barreau et al., NPA 402, 515 (1983)

#### **Shell model**

In a spherically symmetric potential, the eigenstates can be labeled using the total angular momentum.

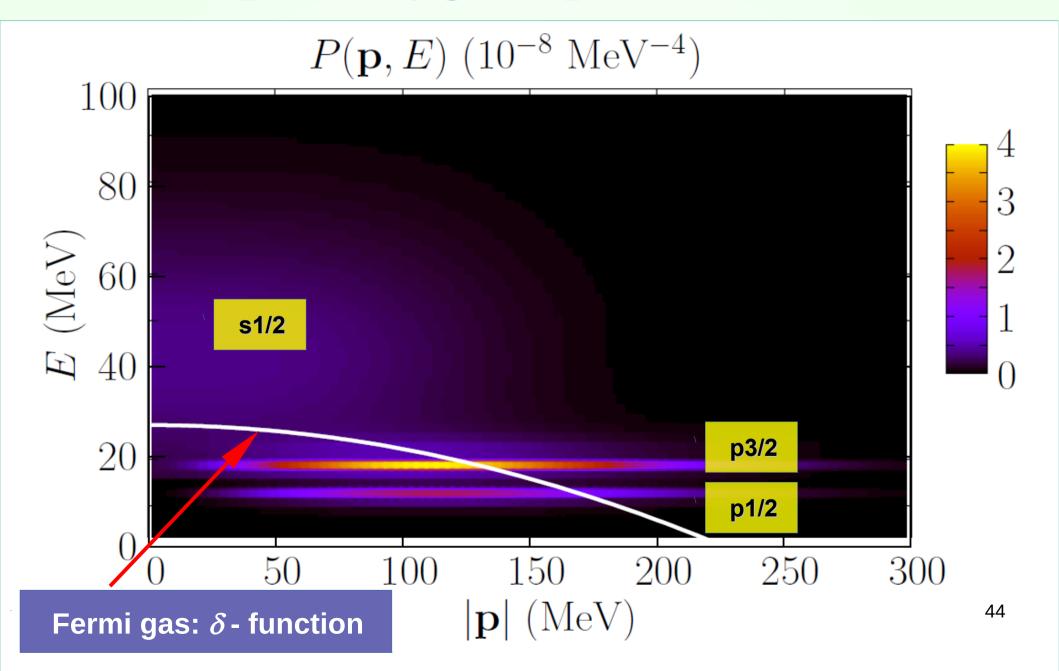


# Example: oxygen nucleus

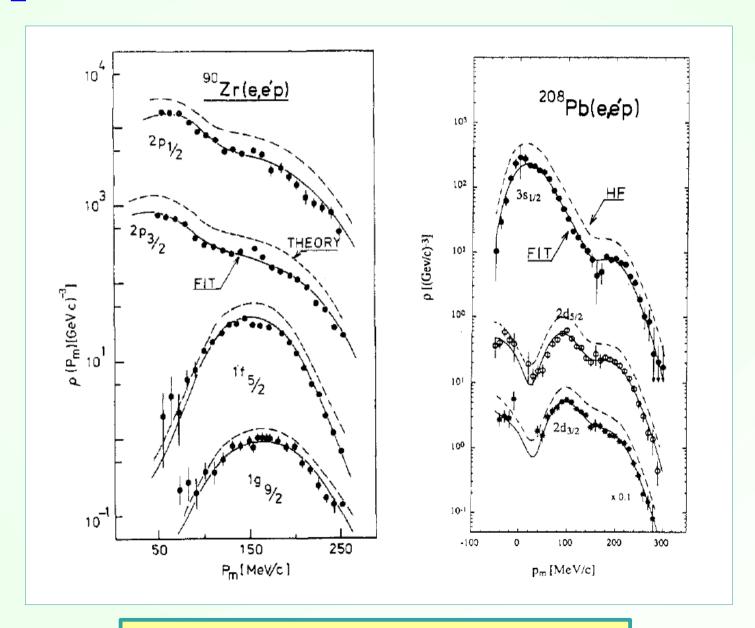


Leuschner et al., PRC 49, 955 (1994)

#### Example: oxygen spectral function



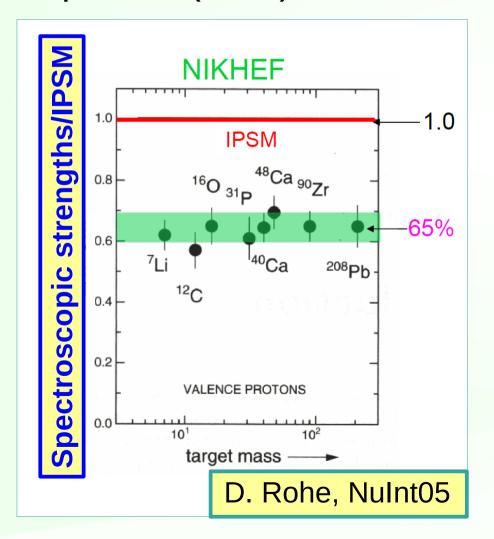
#### **Depletion of the shell-model states**

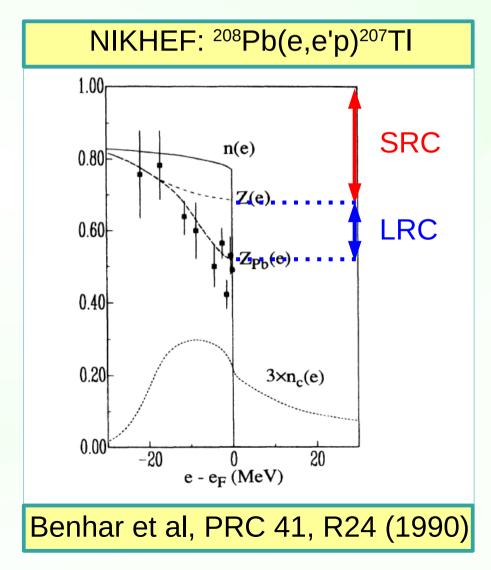


#### Depletion of the shell-model states

The observed depletion is ~35% for the valence shells (LRC and SRC) and ~20% when higher missing energy

is probed (SRC).







# Spectral function approach

The main source of the depletion of the shell-model states at high E are short-range nucleon-nucleon correlations.

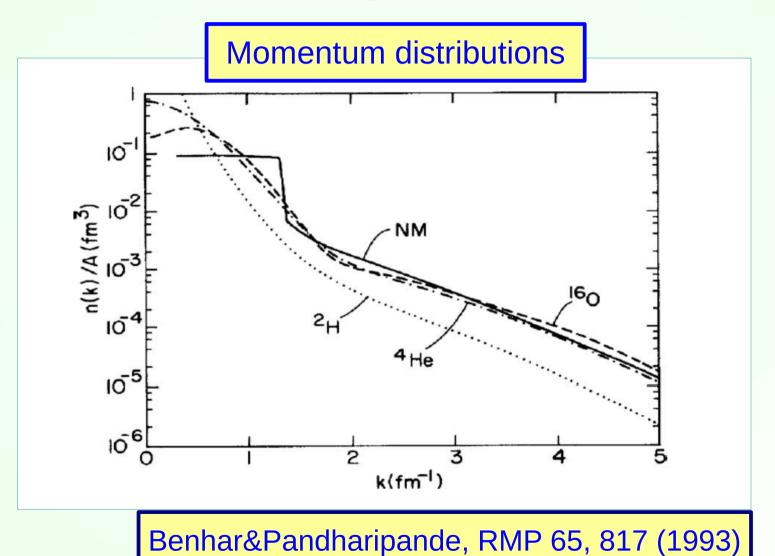
Yielding NN pairs (typically pn pairs) with high relative momentum, they move ~20% of nucleons to the states of high removal energies.

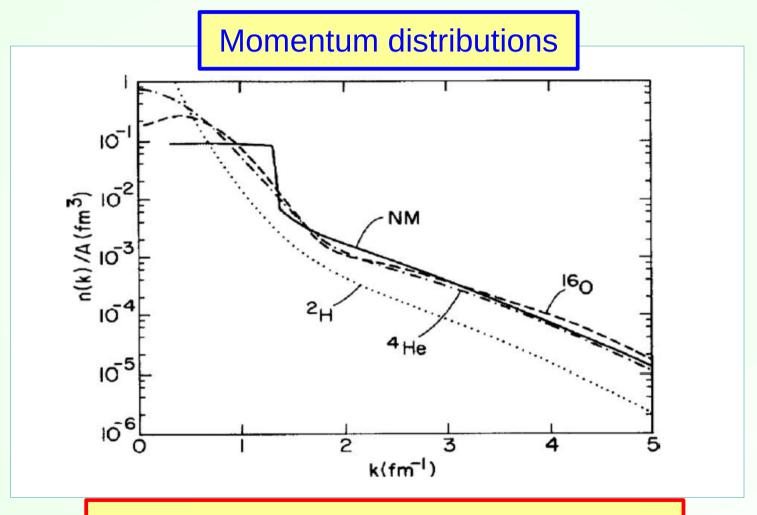
The hole spectral function can be expressed as

$$P_N(\mathbf{p}, E) = \sum_{\alpha} n_{\alpha} |\phi_{\alpha}|^2 f_{\alpha}(E - E_{\alpha}^N) + P_{\text{corr}}^N(\mathbf{p}, E),$$

describes the contribution of the shell-model states, vanishes at high |p| or high *E* 

relevant only at high |p| and E

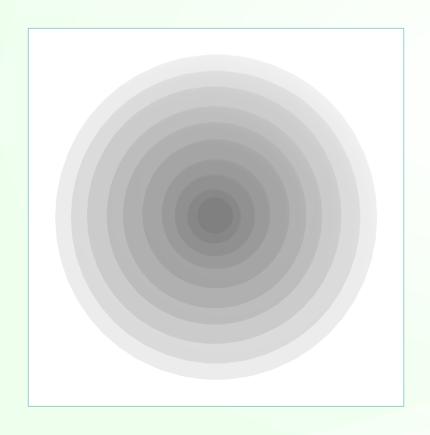




SRC don't depend on the shell structure or finite-size effects, only on the density

### Local-density approximation

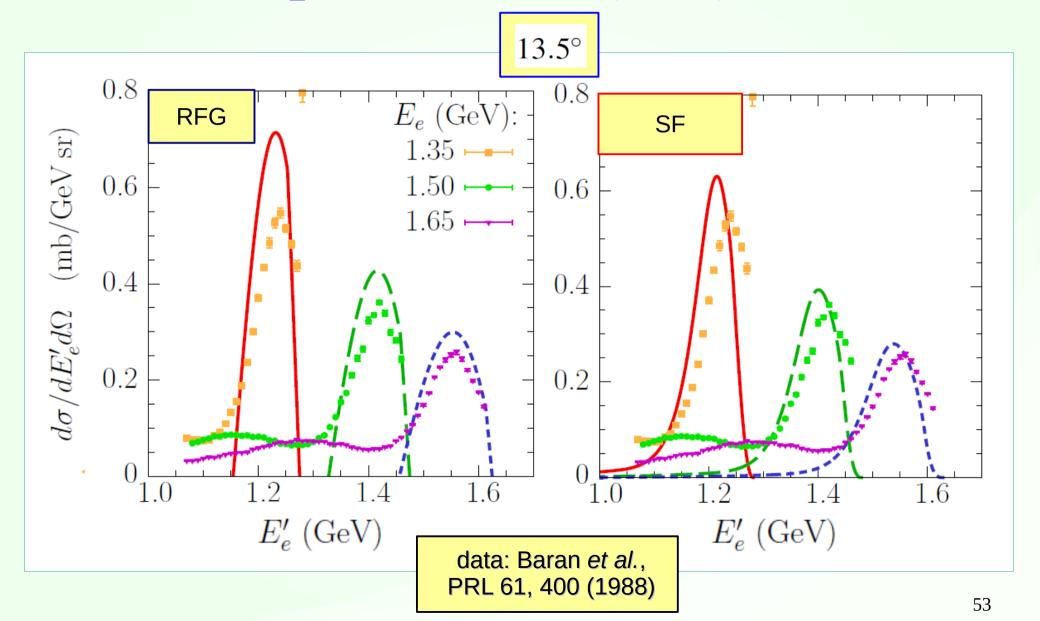
The correlation component in nuclei can be obtained combining the results for infinite nuclear matter obtained at different densities:



$$P_{\text{corr}}^{N}(\mathbf{p}, E) = \int dR \rho(R) P_{\text{corr}}^{NM,N}(\rho, \mathbf{p}, E).$$

Benhar et al., NPA 579 493, (1994)

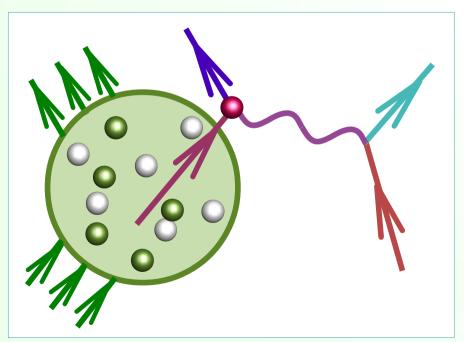
#### Comparison to C(e, e') data



$$E_{\mathbf{k}} + M_A = E_{\mathbf{k}'} + E_{A-1} + E_{\mathbf{p}'}$$

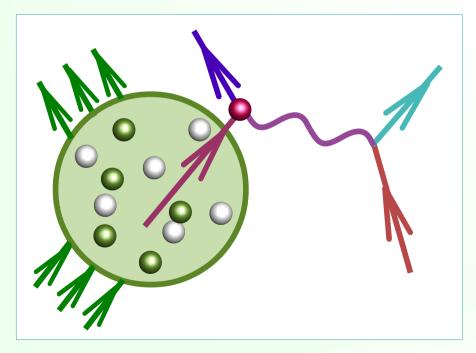
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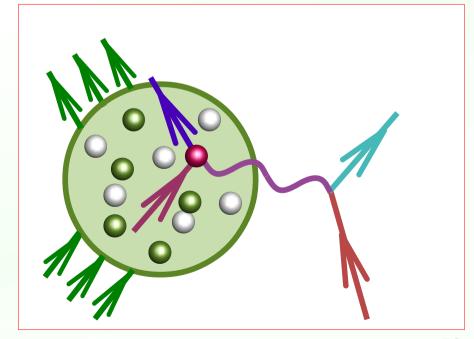




$$E_{\mathbf{k}} + M_A = E_{\mathbf{k}'} + E_{A-1} + E_{\mathbf{p}'}$$





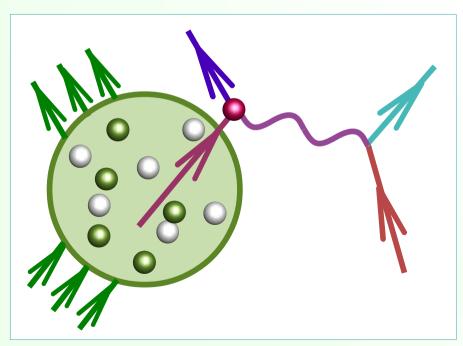


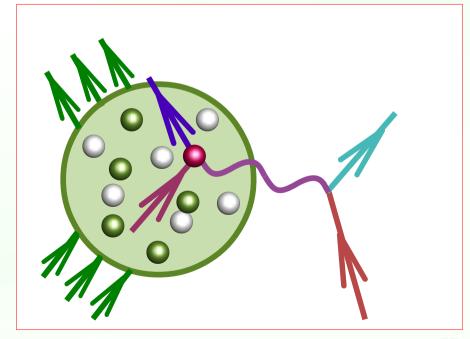
$$E_{\mathbf{k}} + M_A = E_{\mathbf{k}'} + E_{A-1} + E_{\mathbf{p}'}$$



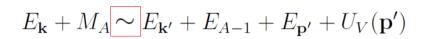






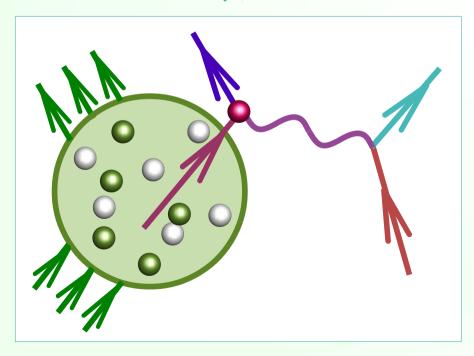


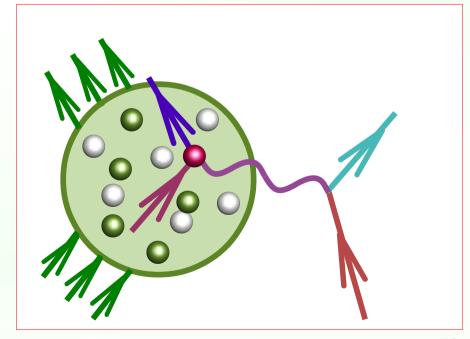
$$E_{\mathbf{k}} + M_A = E_{\mathbf{k}'} + E_{A-1} + E_{\mathbf{p}'}$$











#### **Final-state interactions**

Their effect on the cross section is easy to understand in terms of the complex optical potential:

- the real part modifies the struck nucleon's energy spectrum: it differes from  $\sqrt{M^2 + p'^2}$
- the imaginary part reduces the single-nucleon final states and produces multinucleon final states

$$e^{i(E+U)t} = e^{i(E+U_V)t}e^{-U_W t}$$

Horikawa et al., PRC 22, 1680 (1980)

#### **Final-state interactions**

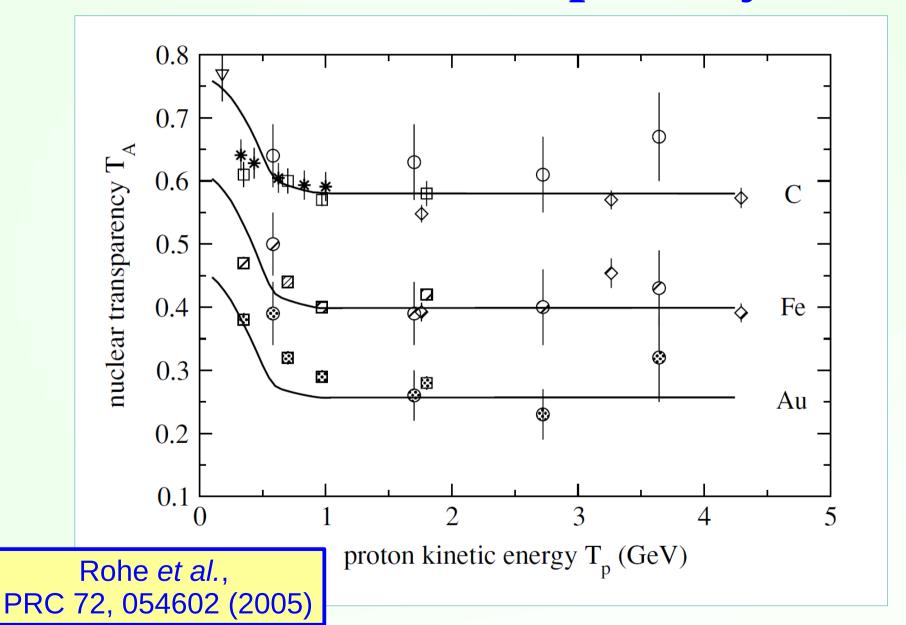
In the convolution approach,

$$\frac{d\sigma^{\text{FSI}}}{d\omega d\Omega} = \int d\omega' f_{\mathbf{q}}(\omega - \omega') \frac{d\sigma^{\text{IA}}}{d\omega' d\Omega},$$

with the folding function

$$f_{\mathbf{q}}(\omega) = \delta(\omega)\sqrt{T_A} + \left(1-\sqrt{T_A}\right)F_{\mathbf{q}}(\omega),$$
 Nucl. transparency

#### **Nuclear transparency**



### Real part of the optical potential

We account for the spectrum modification by

$$f_{\mathbf{q}}(\omega - \omega') \to f_{\mathbf{q}}(\omega - \omega' - U_V).$$

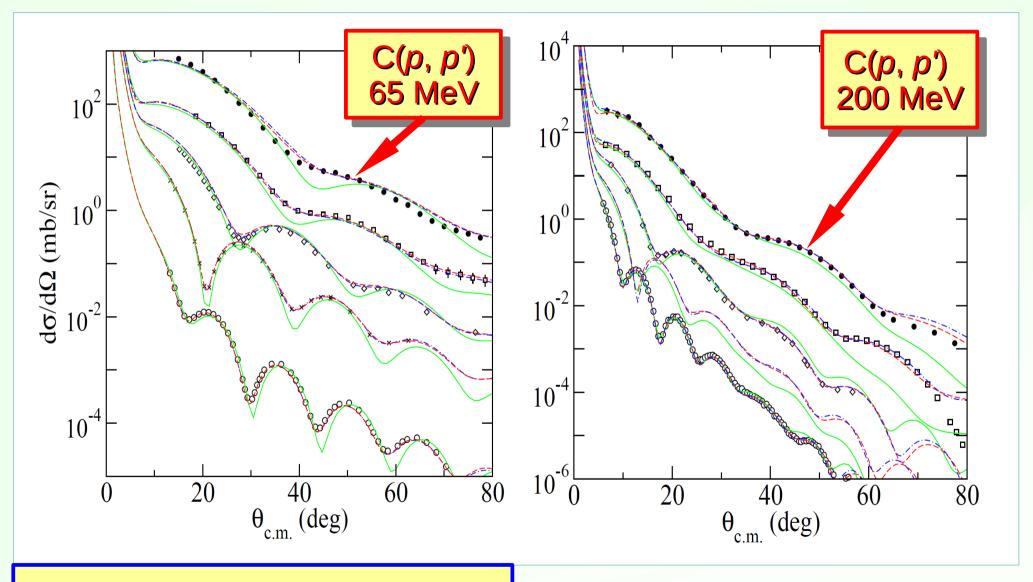
This procedure is similar to that from the Fermi gas model to introduce the binding energy in the argument of  $\delta(...)$ .

$$U_V = U_V(t_{\rm kin})$$

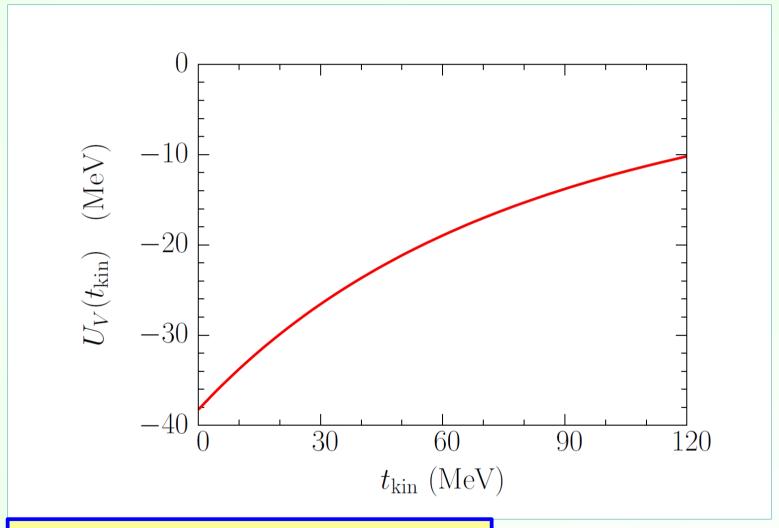
$$U_V = U_V(t_{\rm kin})$$

$$t_{\rm kin} = \frac{E_{\mathbf{k}}^2(1 - \cos \theta)}{M + E_{\mathbf{k}}(1 - \cos \theta)}$$

#### Optical potential by Cooper et al.



#### Optical potential by Cooper et al.



obtained from Cooper *et al.*, PRC 47, 297 (1993)

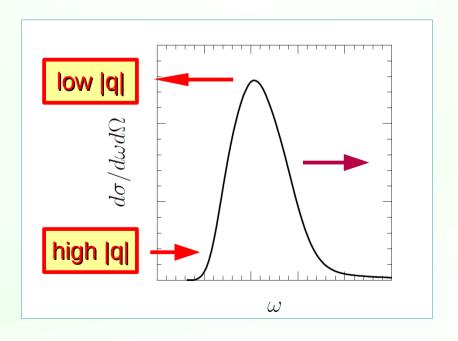
#### Simple comparison

#### Real part of the OP

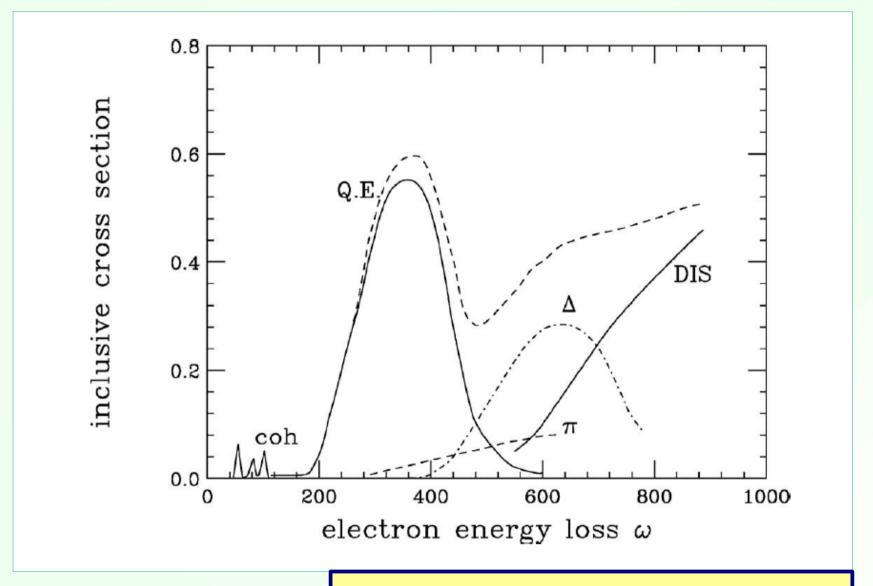
- acts in the final state
- shifts the QE peak to low ω at low |q|
   (to high ω at high |q|)

#### Binding energy in RFG

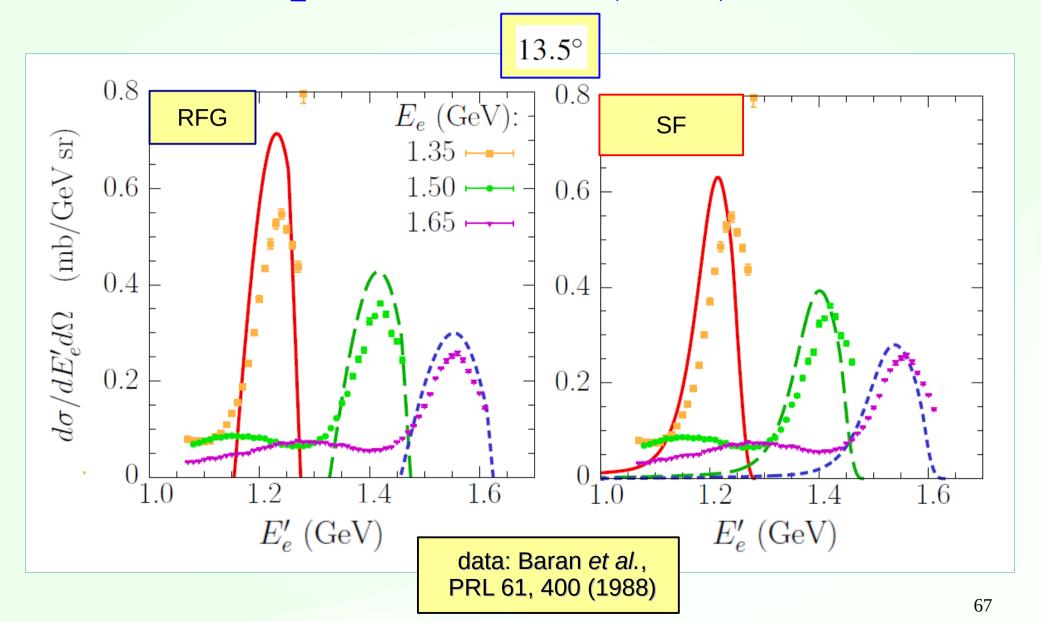
- acts in the initial state
- shifts the QE peak to high  $\omega$



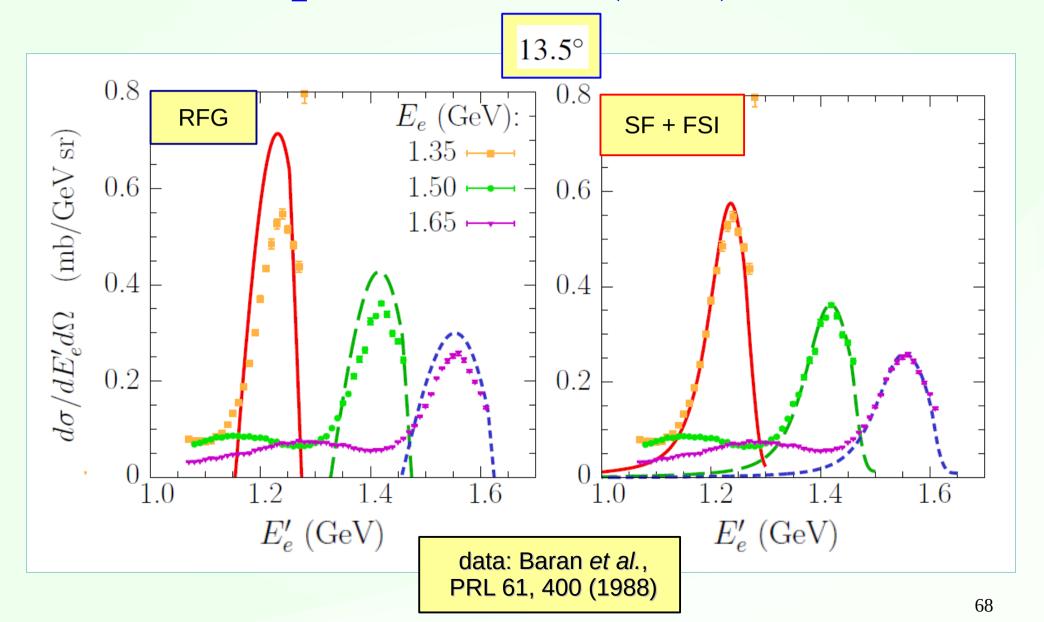
#### Why to focus on quasielastic?



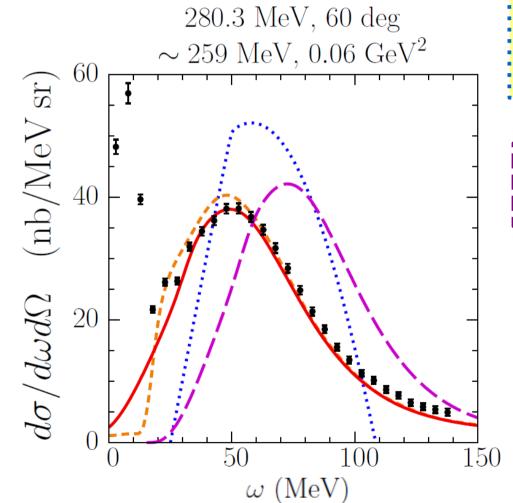
#### Comparison to C(e, e') data



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#### **Compared calculations**



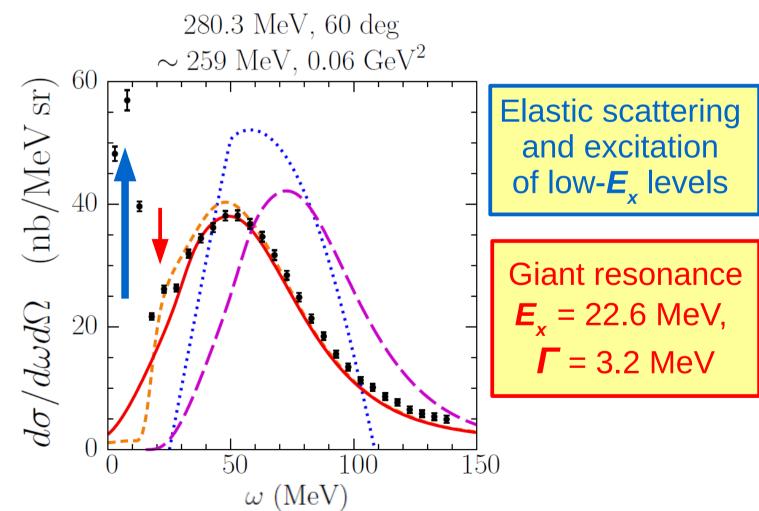
RFG model  $\varepsilon$  = 25 MeV  $p_F$  = 221 MeV

SF calculation without FSI

SF calculation, LDA treatment of Pauli blocking

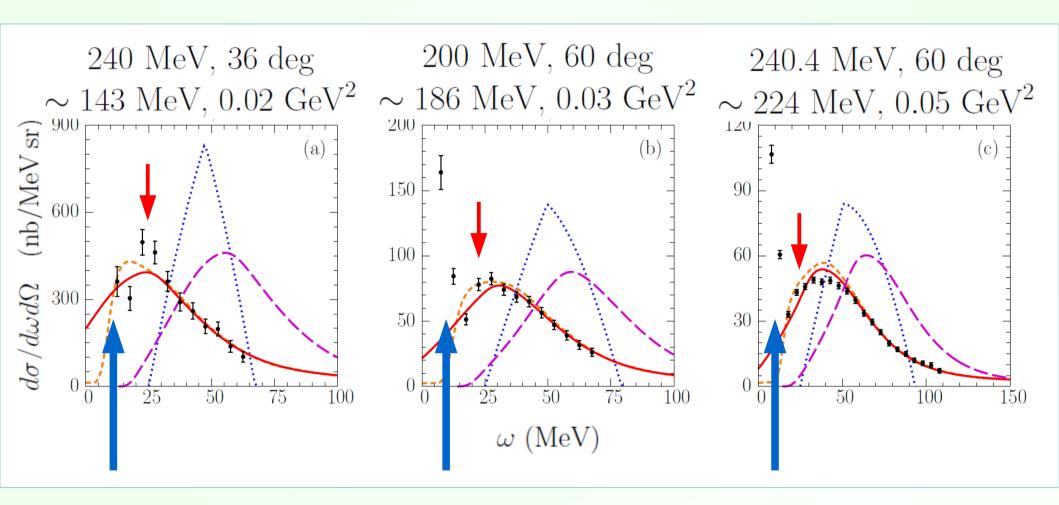
SF calculation, step function

#### **Compared calculations**



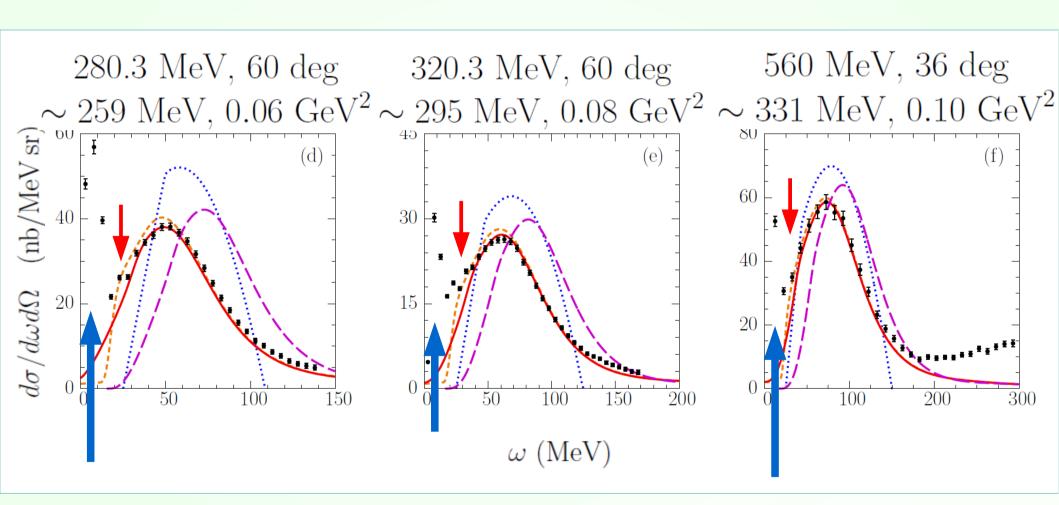
Calcs. include QE by 1-body current only

#### Comparisons to C(e,e') data



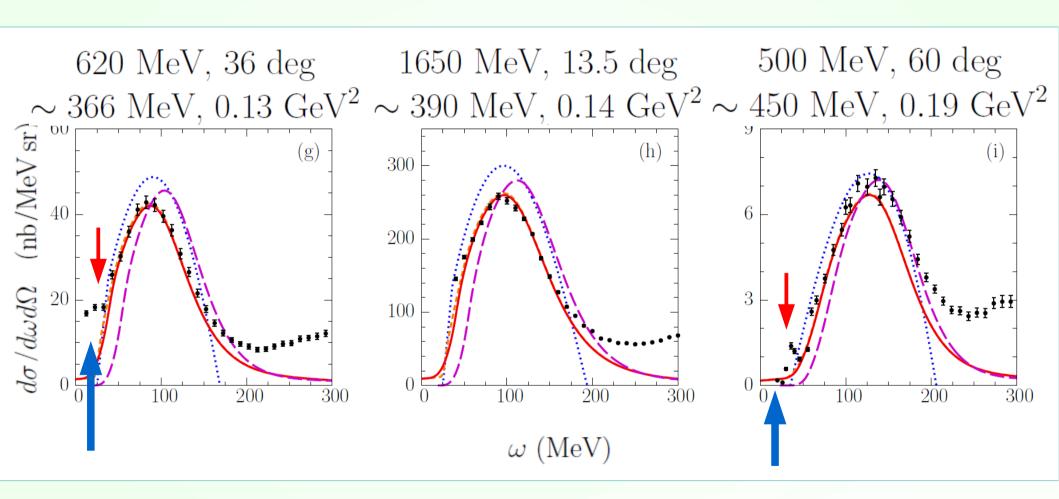
Barreau *et al.*, NPA 402, 515 (1983)

#### Comparisons to C(e,e') data



Barreau *et al.*, NPA 402, 515 (1983)

### Comparisons to C(e,e') data



Barreau *et al.*, NPA 402, 515 (1983) Baran *et al.*, PRL 61, 400 (1988)

Whitney *et al.*, PRC 9, 2230 (1974)

### Comparisons to C(e,e') data

The supplemental material of PRD 91,033005 (2015) shows comparisons to the data sets collected at 54 kinematical setups

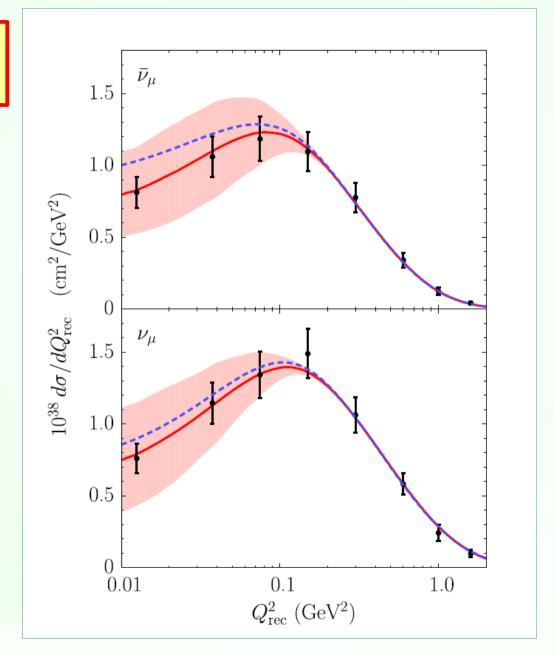
- energies from ~160 MeV to ~4 GeV,
- angles from 12 to 145 degrees,
- at the QE peak, the values of momentum transfer from  $\sim 145$  to  $\sim 1060$  MeV/c and  $0.02 \le Q^2 \le 0.86$  (GeV/c)<sup>2</sup>.

#### **CCQE MINERvA data**

SF calculations with FSI

VS.

SF calculation without FSI



Fields *et al.*, PRL 111, 022501 (2013)

A. M. A., PRD 92, 013007 (2015)

Fiorentini *et al.*, PRL 111, 022502 (2013)

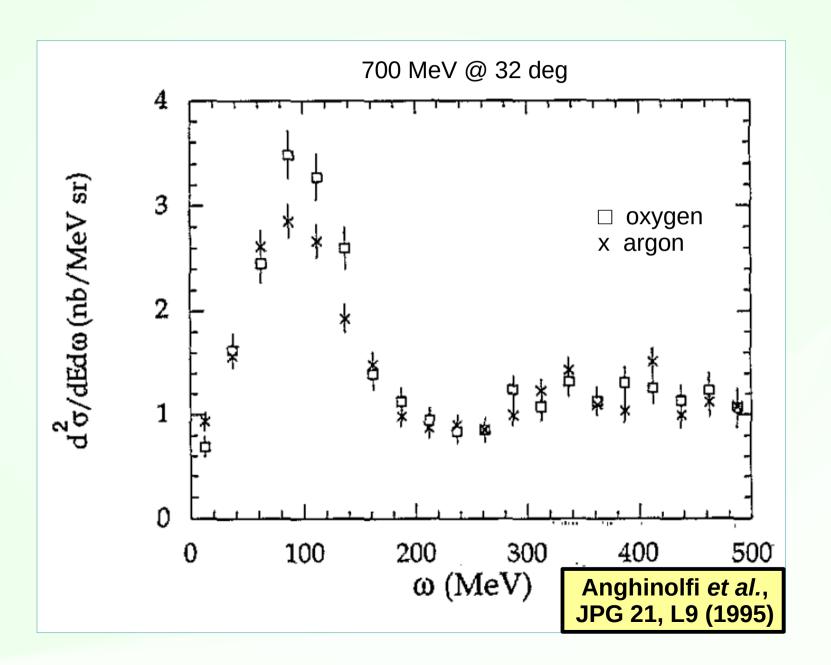
## **CCQE MINERvA data**

TABLE I. Fit results to the CC QE MINERvA data.									
	antineutrino	neutrino	combined fit						
	including theoretical uncertainties:								
$M_A$ (GeV)	$1.16 \pm 0.06$	$1.17 \pm 0.06$	$1.16 \pm 0.06$						
$\chi^2/\text{d.o.f.}$	0.38	1.33	0.93						
	neglectin	neglecting theoretical uncertainties:							
$M_A$ (GeV)	$1.15 \pm 0.10$	$1.15 \pm 0.07$	$1.13 \pm 0.06$						
$\chi^2/\text{d.o.f.}$	0.44	1.38	1.00						
	neglecting FSI ( $M_A = 1.16 \text{ GeV}$ ):								
$\chi^2/\text{d.o.f.}$	2.49	2.45	2.42						



Measurement of the spectral function of argon in JLab

#### What do we know about Ar?



#### What do we know about Ar?

nuclear excitations by up to ~11 MeV
 Cameron & Singh, Nucl. Data Sheets 102, 293 (2004)

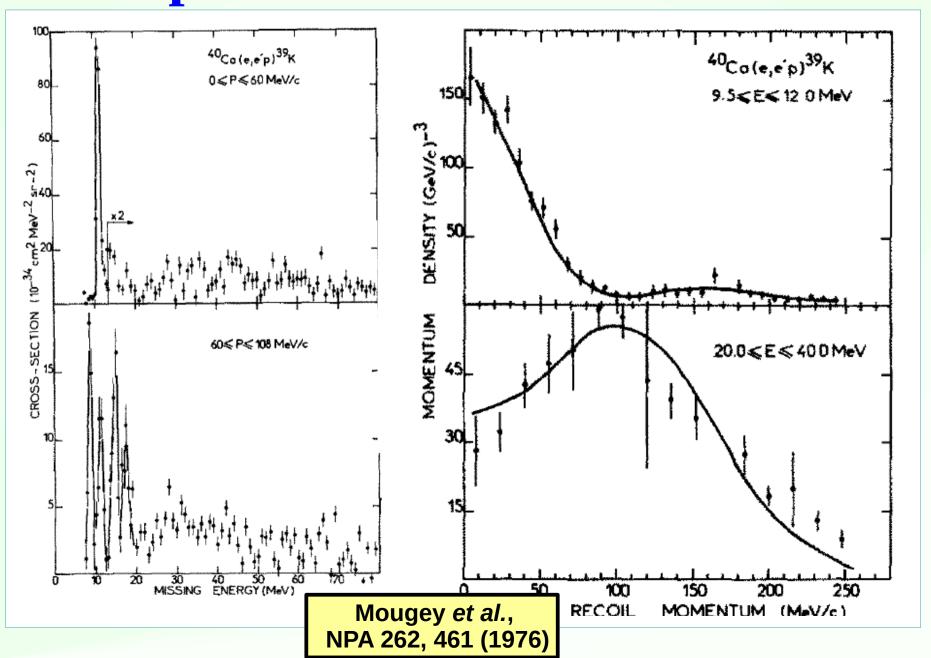
angular distributions of <sup>40</sup>Ar(p, p') for a few excitation lvls.
 Fabrici et al., PRC 21, 830 & 844 (1980); De Leo et al.,
 PRC 31, 362 (1985); Blanpied et al., PRC 37, 1304 (1988)

angular distributions of <sup>40</sup>Ar(*p*, *d*)<sup>39</sup>Ar
 Tonn *et al.*, PRC **16**, 1357 (1977)

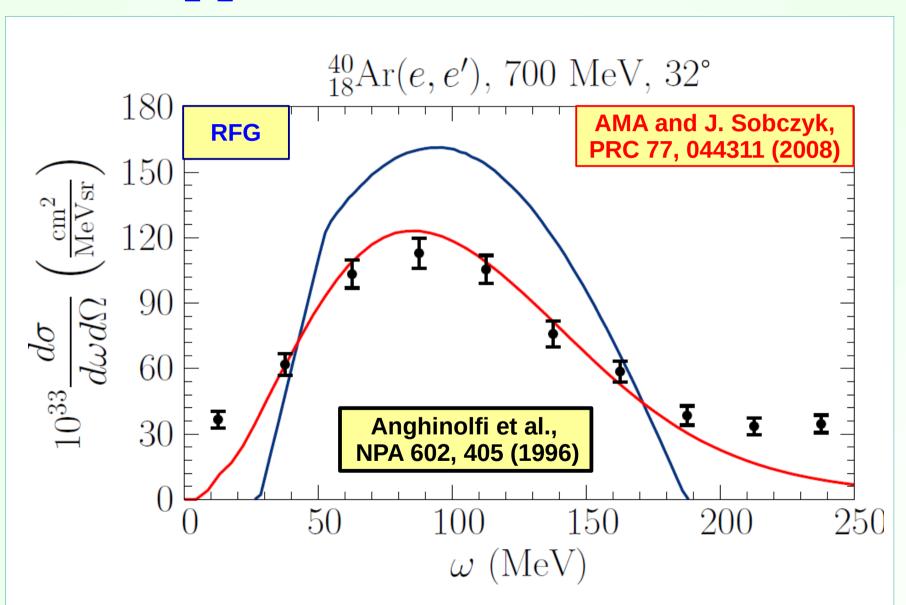
#### What do we know about Ar?

- n-Ar total cross section form energies < 50 MeV</li>
   Winters et al., PRC 43, 492 (1991)
- $^{40}$ Ar( $\nu_e$ , e) cross section from the mirror  $^{40}$ Ti  $\rightarrow$   $^{40}$ Sc decay Bhattacharya et al., PRC **58**, 3677 (1998)
- Gammov-Teller strength distrib. for  $^{40}$ Ar  $\rightarrow$   $^{40}$ K from  $0^{\circ}(p, n)$ Bhattacharya *et al.*, PRC **80**, 055501 (2009)
- 40Ar(n, p)40Cl cross section between 9 and 15 MeV
   Bhattacharya et al., PRC 86, 041602(R) (2012)

## Spectral function of <sup>40</sup>Ca



### Approximated SF of <sup>40</sup>Ar



### Experiment E12-14-012 at JLab

"We propose a measurement of the coincidence (e,e'p) cross section on argon. This data will provide the experimental input indispensable to construct the argon spectral function, thus paving the way for a reliable estimate of the neutrino cross sections."

Benhar *et al.*, arXiv:1406.4080

#### Experiment E12-14-012 at JLab

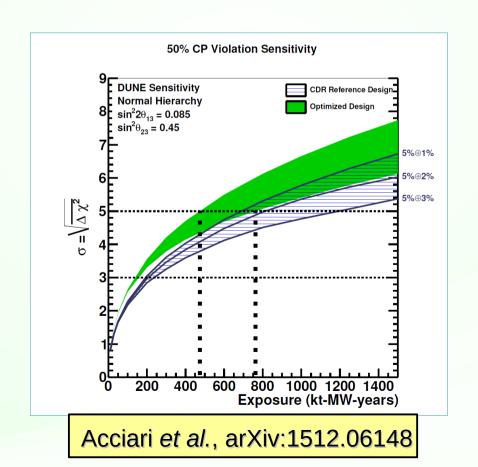
Primary goal: extraction of the proton shell structure of  $^{40}$ Ar from (e,e'p) scattering

- spectroscopic factors,
- energy distributions,
- momentum distributions.

Secondary goal: improved description of final-state interactions in the argon nucleus.

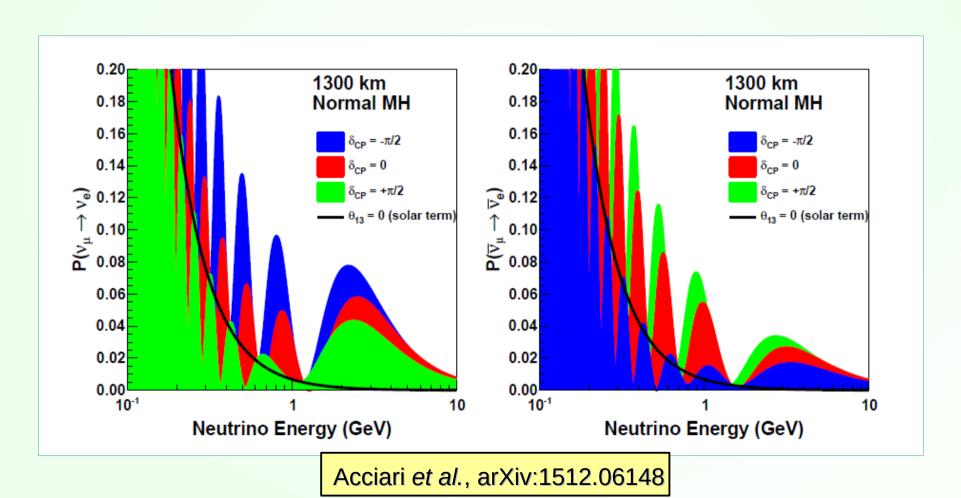
### **Physics motivation**

Expected sensitivity of DUNE to CP violation as a function of exposure for a  $v_e$  signal normalization uncertainties between 5% + 1% and 5% + 3%.



### **Physics motivation**

Appearance probability as a function of neutrino energy



86

#### **Relevance for DUNE**

#### Neutrino oscillations

Reduction of systematic uncertainties from nuclear effects, especially for the 2nd oscillation maximum.

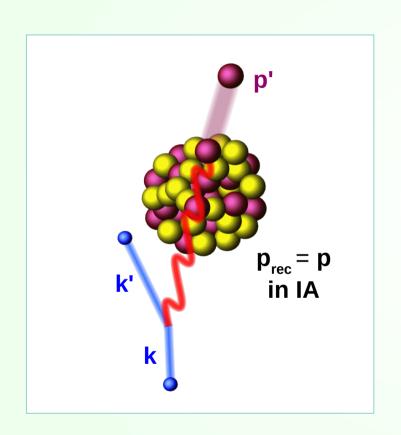
#### Proton decay

Probed lifetime affected by the partial depletion of the shell-model states.

#### Supernova neutrinos

Information on the valence shells essential for accurate simulations and detector design.

#### Impulse approximation



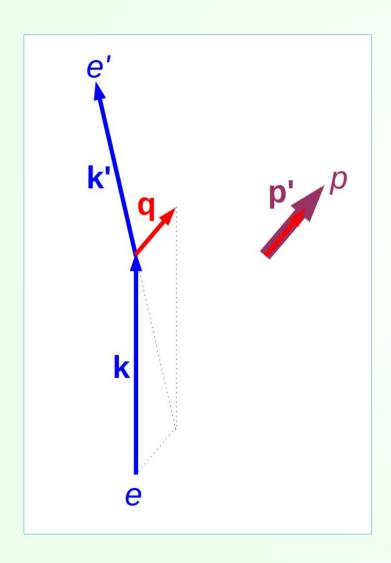
$$\frac{d^6 \sigma_{\rm IA}}{d\Omega_{k'} dE_{k'} d\Omega_{p'} dE_{p'}} \propto \sigma_{ep} \, S(\mathbf{p}, E) \, T_A(E_{p'})$$

 $\sigma_{ep}$  elementary cross section

 $S(\mathbf{p}, E)$  spectral function

 $T_A(E_{p'})$  nuclear transparency

# (Anti)parallel kinematics, p' | q



#### **Energy conservation**

$$E_{\mathbf{k}} + M_A = E_{\mathbf{k'}} + E_{\mathbf{p'}} + \sqrt{(M_A - M + E)^2 + \mathbf{p}_{\text{rec}}^2}$$

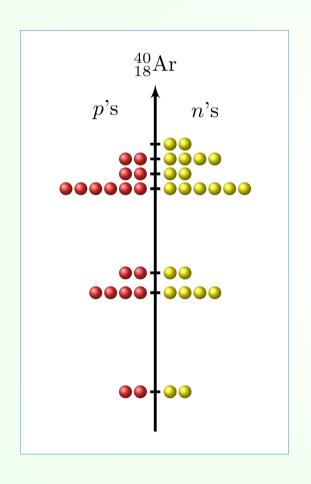
#### Momentum conservation

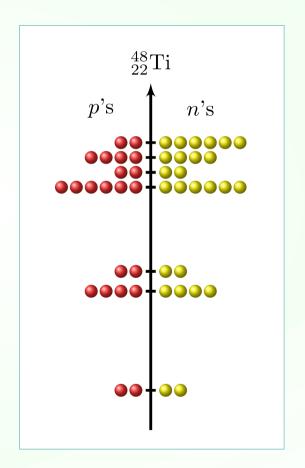
$$\mathbf{q} = \mathbf{p'} + \mathbf{p}_{\mathrm{rec}} 
ightarrow |\mathbf{q}| = |\mathbf{p'}| + |\mathbf{p}_{\mathrm{rec}}|$$

$$\mathbf{q} = \mathbf{p}' + \mathbf{p}_{\mathrm{rec}} 
ightarrow |\mathbf{q}| = |\mathbf{p}'| - |\mathbf{p}_{\mathrm{rec}}|$$

Impulse Approximation,  $|p_{rec}| = |p|$ 

## Neutron spectral function of <sup>40</sup>Ar



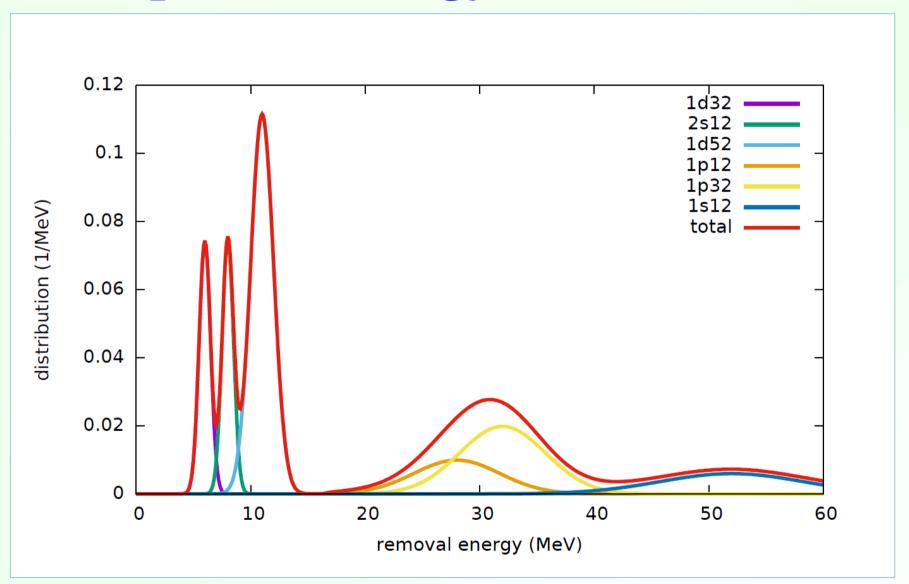


## **Kinematic settings**

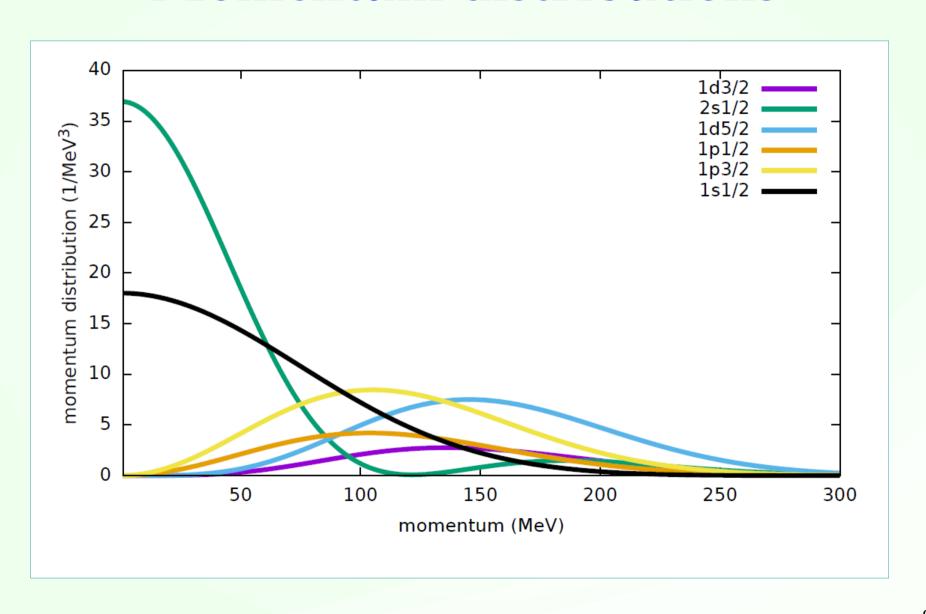
	$E_e$	$E_{e'}$	$\theta_e$	$P_p$	$\theta_p$	$ \mathbf{q} $	$p_m$	Ar	Ti
	MeV	MeV	$\deg$	MeV/c	$\deg$	MeV/c	$\mathrm{MeV}/c$	events	events
kin1	2222	1799	21.5	915	-50.0	857.5	57.7	44M	13M
kin2	2222	1716	20.0	1030	-44.0	846.1	183.9	63M	21M
kin3	2222	1799	17.5	915	-47.0	740.9	174.1	73M	28M
kin4	2222	1799	15.5	915	-44.5	658.5	229.7	159M	113M
kin5	2222	1716	15.5	1030	-39.0	730.3	299.7	45M	61k
(e, e')	2222		15.5					3M	3M

**Data collected Feb - Mar 2017** 

### **Expected energy distributions**



#### **Momentum distributions**

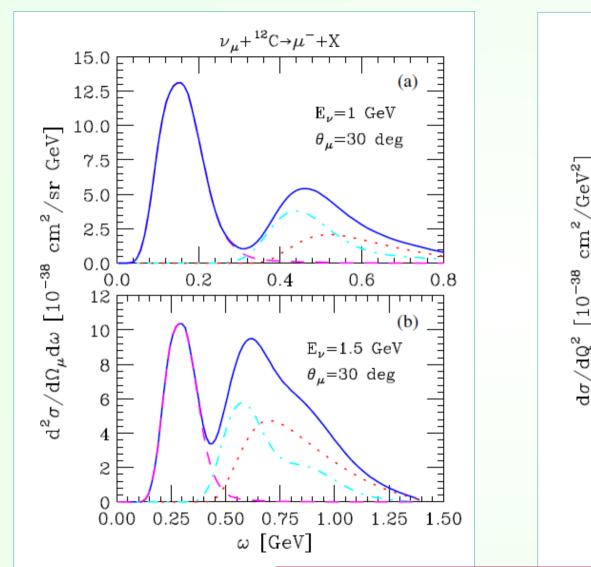


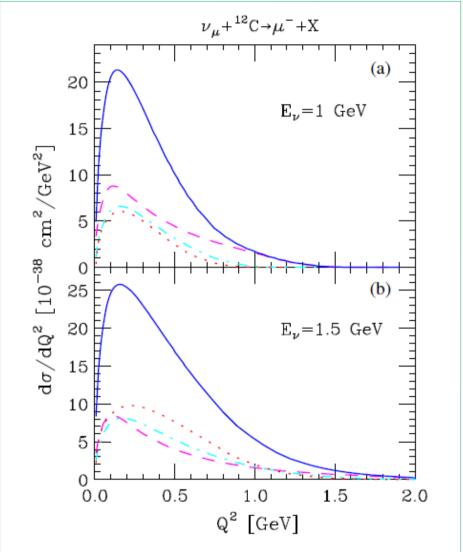
#### **Summary**

- An accurate description of nuclear effects, including finalstate interactions, is crucial for an accurate reconstruction of neutrino energy.
- Theoretical models **must be validated** against (*e,e'*) data to estimate their uncertainties.
- The spectral function formalism can be used in Monte Carlo simulations to improve the accuracy of description of nuclear effects.
- **JLab experiment** will provide an input to estimate the spectral function of argon, essential for the next generation of neutrino-oscillation experiments.

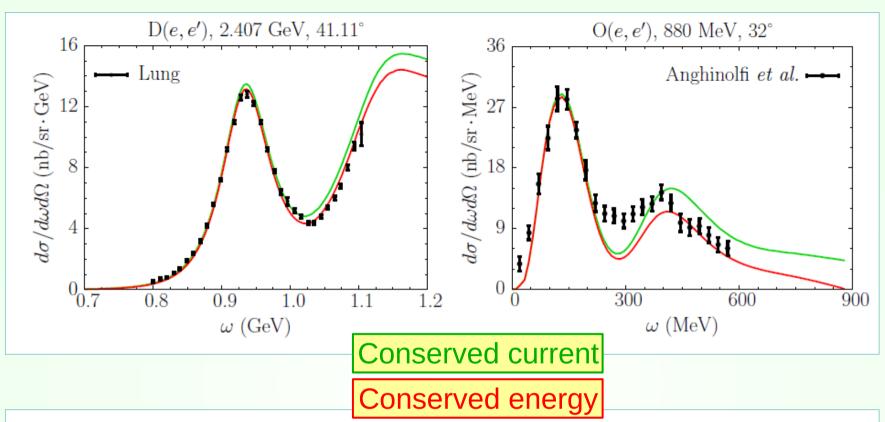


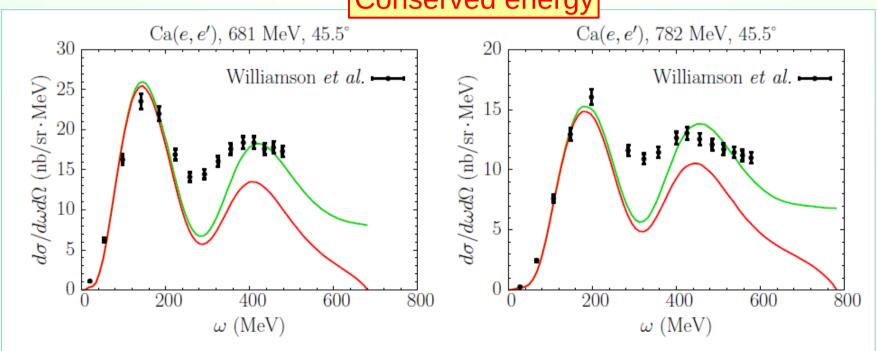
**Backup slides** 

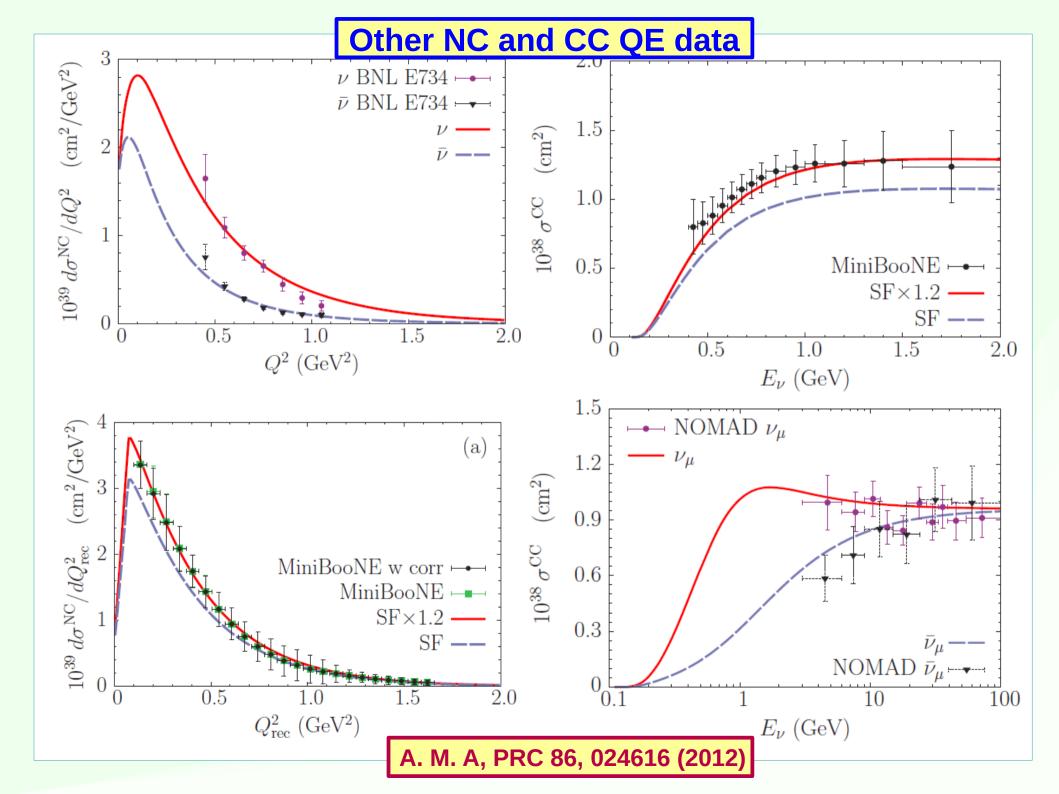




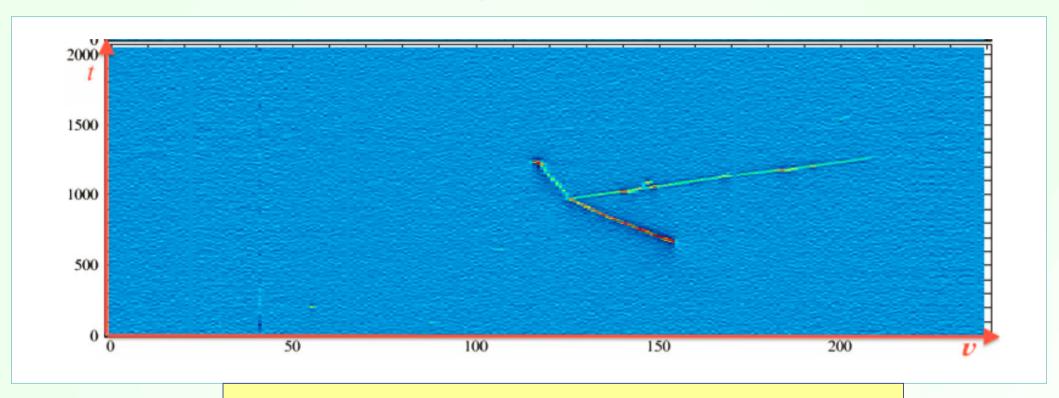
Vagnoni et al., PRL 118, 142502 (2017)







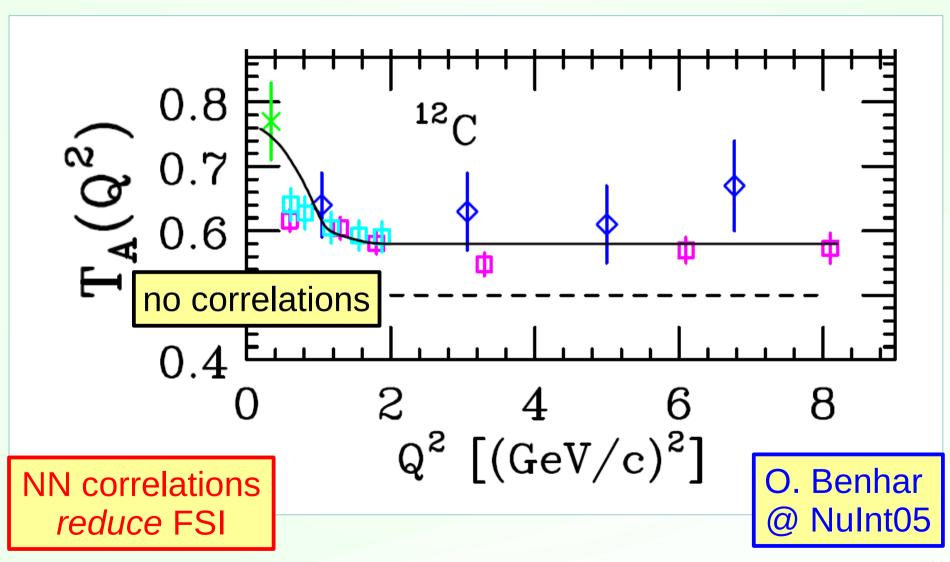
## **Short-range correlations**



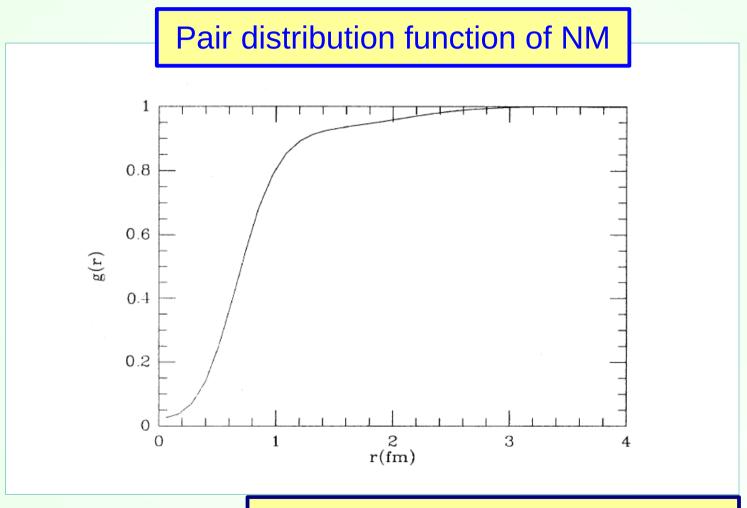
Acciari et al. (ArgoNeuT), PRD 90, 012008 (2014)

Not SRC, simple  $\pi$  reabsorption: Weinstein *et al.*, PRC 94, 045501 (2016)

#### **Nuclear transparency**



### **Short-range correlations**



Benhar et al., PRC 44, 2328 (1991)

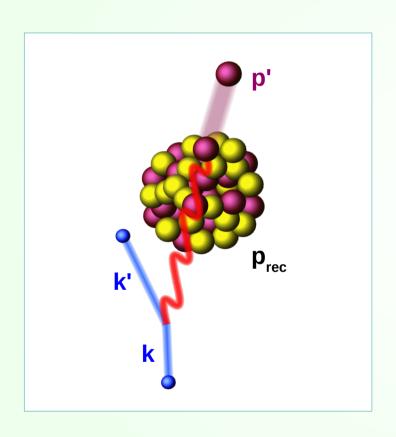
## Why the beam energy ~2 GeV?

	$E_e$	$E_{e'}$	$\theta_e$	$P_p$	$\theta_p$	$ \mathbf{q} $	$p_m$
	MeV	MeV	deg	MeV/c	deg	MeV/c	MeV/c
A	2200	1777	23.01	915	-50.9	895	20
В	2200	1777	21.66	915	-50.1	855	60
$\mathbf{C}$	2200	1777	20.29	915	-49.1	815	100
D	2200	1777	18.90	915	-48.0	775	140
$\mathbf{E}$	2200	1777	17.49	915	-46.6	735	180
F	2200	1777	16.03	915	-44.9	695	220
$\mathbf{G}$	2200	1777	14.53	915	-42.9	655	260
Η	2200	1777	12.96	915	-40.4	615	300
Ι	2200	1777	11.30	915	-37.3	575	340
J	2200	1777	27.64	915	-52.8	1035	-120

## Why the beam energy ~2 GeV?

	$E_e$	$E_{e'}$	$\theta_e$	$P_p$	$\theta_p$	$ \mathbf{q} $	$p_m$
	MeV	MeV	$\deg$	MeV/c	$\deg$	MeV/c	MeV/c
A	4400	3977	10.82	915	-56.5	895	20
В	4400	3977	10.19	915	-55.4	855	60
$\mathbf{C}$	4400	3977	9.55	915	-54.1	815	100
D	4400	3977	8.90	915	-52.6	775	140
$\mathbf{E}$	4400	3977	8.24	915	-50.8	735	180
F	4400	3977	7.56	915	-48.8	695	220
G	4400	3977	6.85	915	-46.4	655	260
Η	4400	3977	6.12	915	-43.6	615	300
Ι	4400	3977	5.34	915	-40.1	575	340
J	4400	3977	12.97	915	-59.6	1035	-120

## Coincidence electron scattering



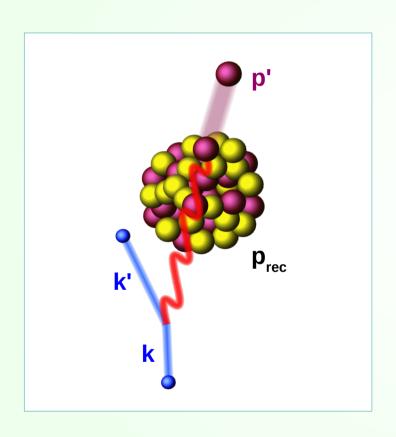
#### **Energy conservation**

$$E_{\mathbf{k}} + M_A = E_{\mathbf{k'}} + E_{\mathbf{p'}} + \sqrt{(M_A - M + E)^2 + \mathbf{p}_{rec}^2}$$

#### Momentum conservation

$$\mathbf{k} = \mathbf{k}' + \mathbf{p}' + \mathbf{p}_{\rm rec}$$

# (Anti)parallel kinematics, p' q



#### **Energy conservation**

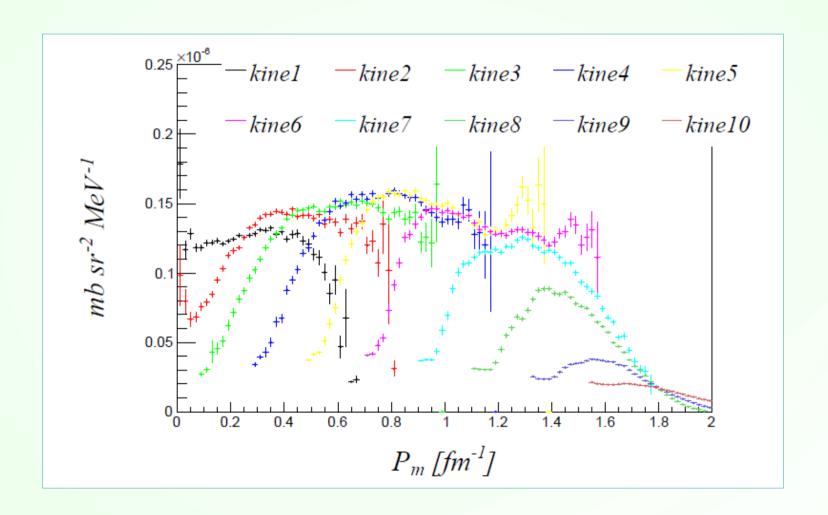
$$E_{\mathbf{k}} + M_A = E_{\mathbf{k'}} + E_{\mathbf{p'}} + \sqrt{(M_A - M + E)^2 + \mathbf{p}_{\text{rec}}^2}$$

#### Momentum conservation

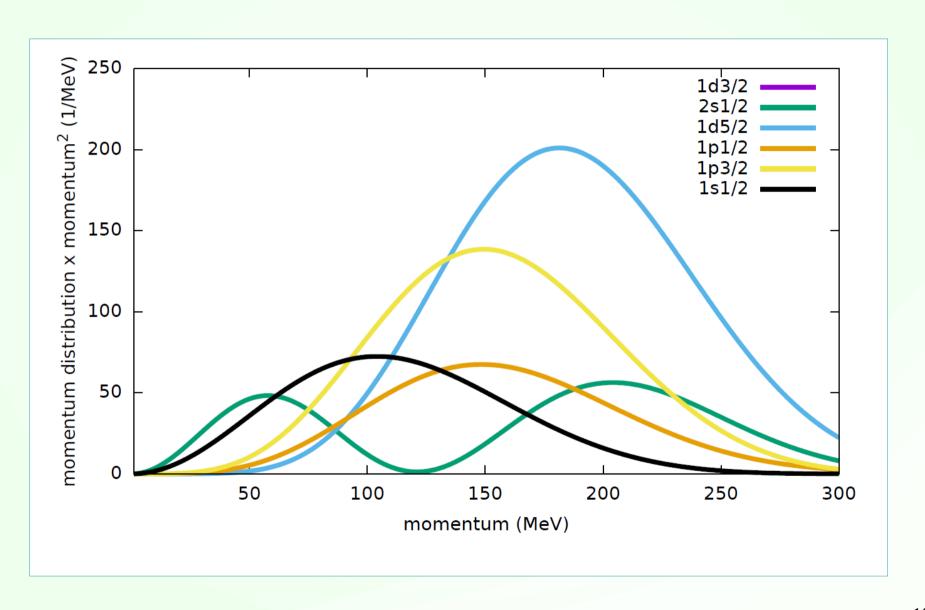
$$\mathbf{q} = \mathbf{p'} + \mathbf{p}_{\mathrm{rec}} 
ightarrow |\mathbf{q}| = |\mathbf{p'}| + |\mathbf{p}_{\mathrm{rec}}|$$

$$\mathbf{q} = \mathbf{p}' + \mathbf{p}_{\mathrm{rec}} 
ightarrow |\mathbf{q}| = |\mathbf{p}'| - |\mathbf{p}_{\mathrm{rec}}|$$

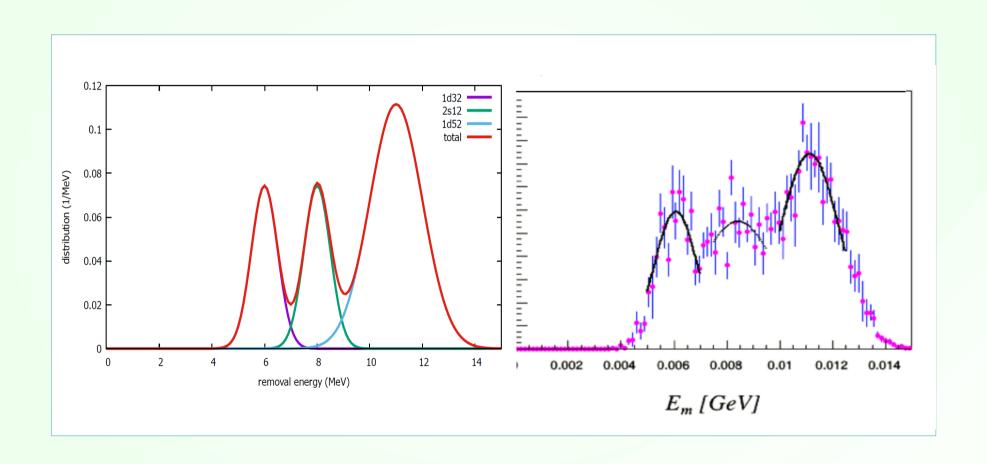
### **Optimizations**



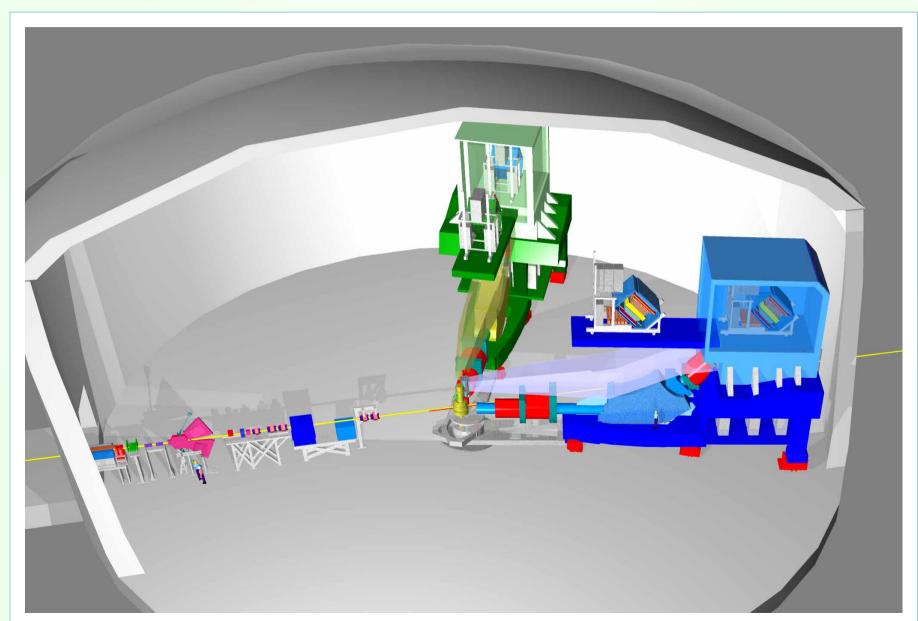
#### **Momentum distributions**



## **Expected energy distributions**



### **Hall A**



# **Argon cell**

